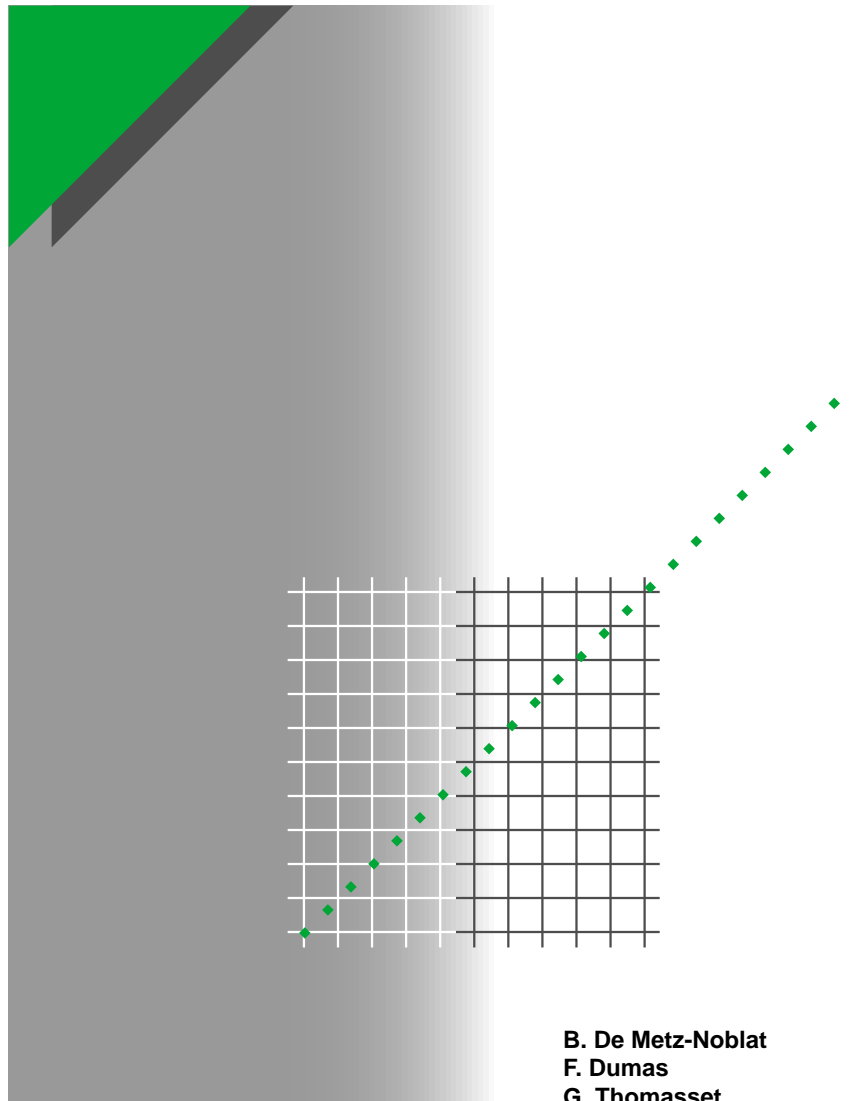


Cahier technique no. 158

Calculation of short-circuit currents



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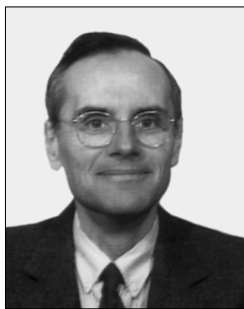
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no. 158

Calculation of short-circuit currents



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Lexicon

Abbreviations

BC	Breaking capacity.
MLVS	Main low voltage switchboard.

Symbols

A	Cross sectional area of conductors.
α	Angle between the initiation of the fault and zero voltage.
c	Voltage factor.
$\cos \varphi$	Power factor (in the absence of harmonics).
e	Electromotive force.
E	Electromotive force (maximum value).
φ	Phase angle (current with respect to voltage).
i	Instantaneous current.
i_a	Alternating sinusoidal component of the instantaneous current.
i_{dc}	Aperiodic component of the instantaneous current.
i_p	Maximum current value (first peak of the fault current).
I	Maximum r.m.s. current.
I_b	Short-circuit breaking current (IEC 60909).
I_k	Steady-state short-circuit current (IEC 60909).
I_k''	Initial short-circuit current (IEC 60909).
I_r	Rated current of a generator.
I_s	Service current.
I_{sc}	Steady-state short-circuit current (I_{sc3} = three-phase, I_{sc2} = two-phase, ...).

λ	Factor depending on the saturation inductance of a generator.
k et K	Constants (tables and graphs).
R_a	Equivalent resistance of the upstream network.
R_L	Line resistance per unit length.
S	Cross-sectional area of conductors.
S_n	Transformer kVA rating.
S_{sc}	Short-circuit power.
t_{min}	Minimum dead time for short-circuit development time, often equal to the time delay of a circuit breaker.
u	Instantaneous voltage.
u_{sc}	Transformer short-circuit voltage in %.
U	Network phase-to-phase voltage with no load.
U_n	Network rated voltage with load.
x	Reactance, in %, of the rotating machines
X_a	Equivalent reactance of the upstream network.
X_L	Line reactance per unit length.
X_{subt}	Reactance in % of rotating machines.
Z_L	Link impedance.
Z_{sc}	Network upstream impedance for a three-phase fault.
Z_{up}	Equivalent impedance of the upstream network
$Z_{(1)}, Z_{(2)}, Z_{(0)}$	Positive-sequence, negative- \emptyset sequence and zero-sequence impedances of a network or an element.

Calculation of short-circuit currents

In view of sizing electrical installation and the required equipment, as well as determining the means required for the protection of life and property, short-circuit currents must be calculated for every point in the network.

This "Cahier Technique" reviews the calculation methods for short-circuit currents as laid down by standards such as IEC 60909. It is intended for radial low-voltage (LV) and high-voltage (HV) circuits.

The aim is to provide a further understanding of the calculation methods, essential when determining short-circuit currents, even when computerised methods are employed.

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1 Introduction

Electrical installations almost always require protection against short-circuits wherever there is an electrical discontinuity. This most often corresponds to points where there is a change in conductor cross-section. The short-circuit current must be calculated at each level in the installation in view of determining the characteristics of the equipment required to withstand or break the fault current.

The flow chart in **figure 1** indicates the procedure for determining the various short-circuit currents and the resulting parameters for the different protection devices.

In order to correctly select and adjust the protection devices, graphs of **figures 2, 3 & 4**

are used. Two values of the short-circuit current must be evaluated:

- the maximum short-circuit current, used to determine:
- the breaking capacity of the circuit breakers;
- the making capacity of the circuit breakers;
- the electrodynamic withstand capacity of the wiring system and switchgear.

The maximum short-circuit current corresponds to a short-circuit in the immediate vicinity of the downstream terminals of the protection device. It must be calculated accurately and used with a safety margin.

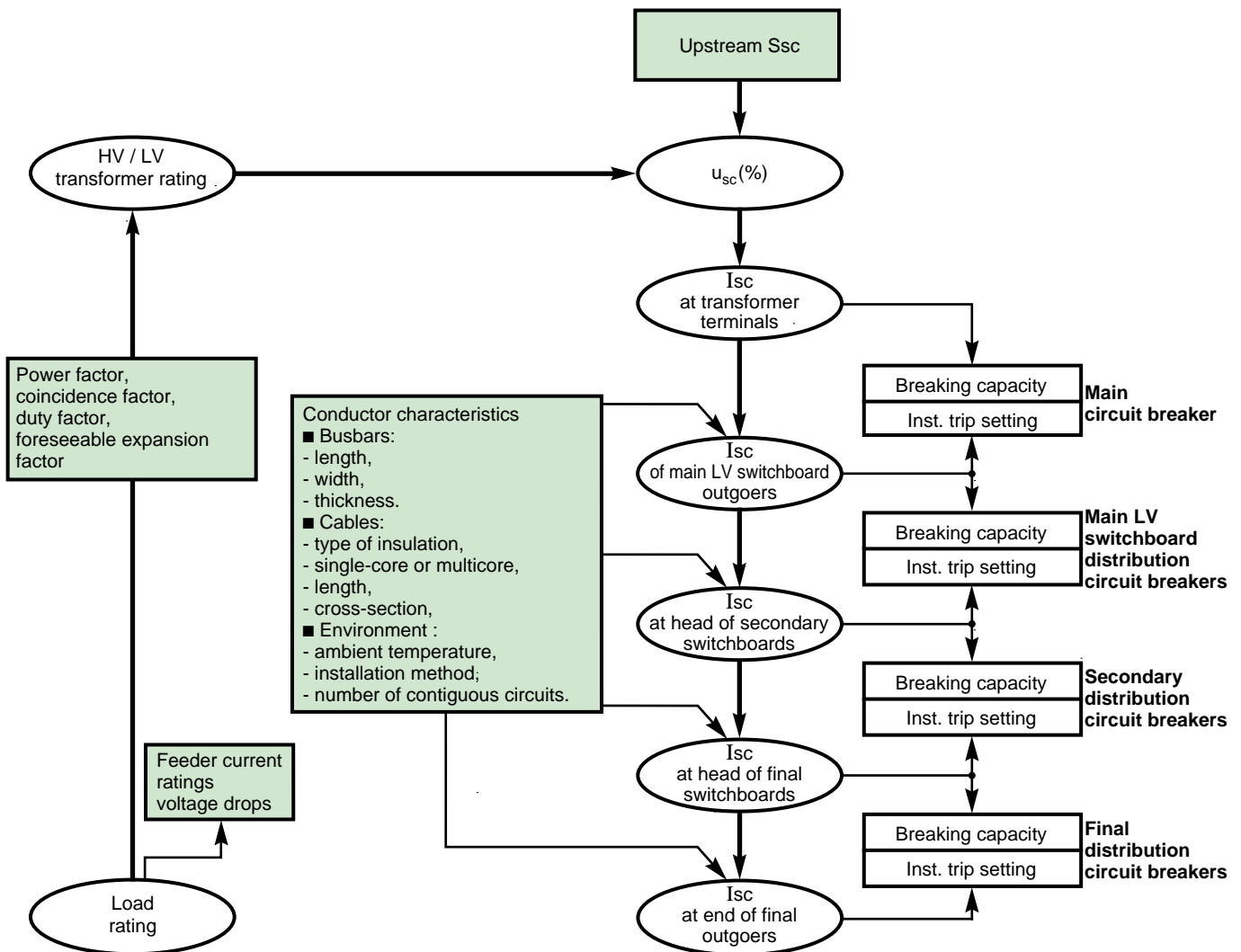


Fig. 1: short-circuit (I_{sc}) calculation procedure when designing an electrical installation.

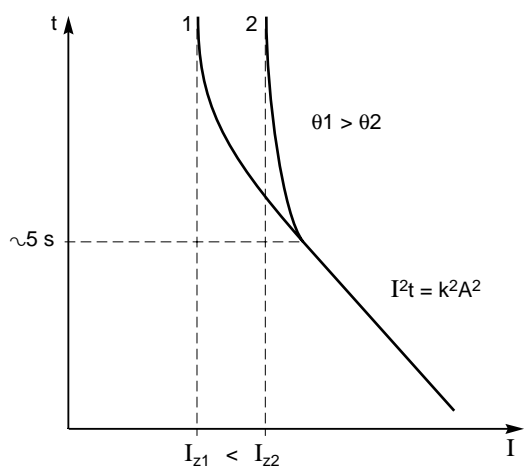


Fig. 2: the I^2t characteristics of a conductor depending on the ambient temperature (temperature of case 1: t_1 being higher than temperature of case 2: t_2 , the admissible current limit I_{z1} is lower than the admissible current limit I_{z2}).

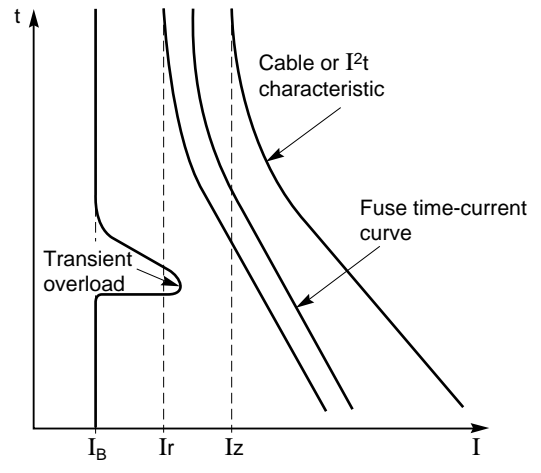


Fig. 4: circuit protection using an aM fuse.

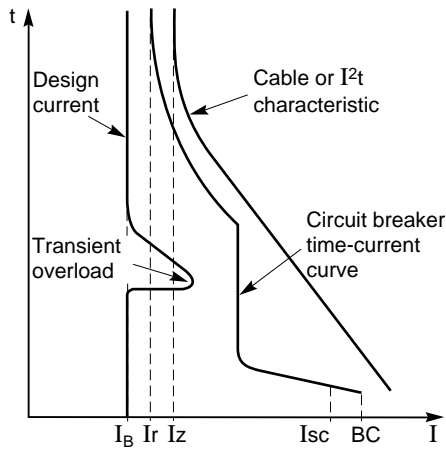


Fig. 3: circuit protection using a circuit breaker.

- the minimum short-circuit current, essential when selecting the time-current curve for circuit breakers and fuses, in particular when:
 - cables are long and/or the source impedance is relatively high (generators, UPSs);

□ protection of life depends on circuit breaker or fuse operation, essentially the case for TN and IT electrical systems.

Note that the minimum short-circuit current corresponds to a short-circuit at the end of the protected line, generally phase-to-earth for LV and phase-to-phase for HV (neutral not distributed), under the least severe operating conditions (fault at the end of a feeder and not just downstream from a protection device, one transformer in service when two can be connected, etc.).

Note also that whatever the case, for whatever type of short-circuit current (minimum or maximum), the protection device must clear the short-circuit within a time t_c that is compatible with the thermal stresses that can be withstood by the protected cable:

$$\int i^2 dt \leq k^2 A^2 \text{ (see fig. 2, 3 and 4)}$$

where A is the cross-sectional area of the conductors and k is a constant calculated on the basis of different correction factors for the cable installation method, contiguous circuits, etc.

Further practical information may be found in the "Electrical Installation Guide" published by Schneider Electric (see the bibliography).

1.1 The main types of short-circuits

Various types of short-circuits can occur in electrical installations.

Characteristics of short-circuits

The primary characteristics are:

- duration (self-extinguishing, transient and steady-state);
- origin:
 - mechanical (break in a conductor, accidental electrical contact between two conductors via a

foreign conducting body such as a tool or an animal);

- internal or atmospheric overvoltages;
- insulation breakdown due to heat, humidity or a corrosive environment;

■ location (inside or outside a machine or an electrical switchboard).

Short-circuits can be:

- phase-to-earth (80 % of faults);

- phase-to-phase (15 % of faults). This type of fault often degenerates into a three-phase fault;
- three-phase (only 5 % of initial faults).

These different short-circuit currents are presented in **figure 5**.

Consequences of short-circuits

The consequences are variable depending on the type and the duration of the fault, the point in the installation where the fault occurs and the short-circuit power. Consequences include:

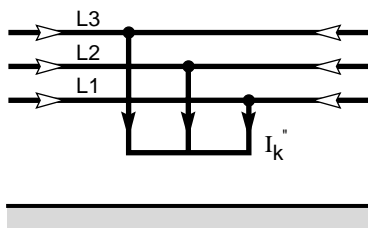
- at the fault location, the presence of electrical arcs, resulting in:
 - damage to insulation;
 - welding of conductors;
 - fire and danger to life;
- on the faulty circuit:
 - electrodynamic forces, resulting in:
 - deformation of the busbars;
 - disconnection of cables;

- excessive temperature rise due to an increase in Joule losses, with the risk of damage to insulation;

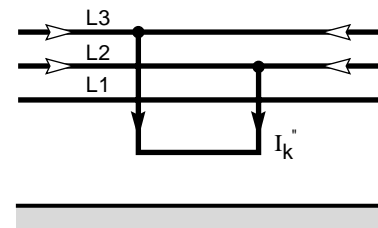
- on other circuits in the network or in near-by networks:

- voltage dips during the time required to clear the fault, ranging from a few milliseconds to a few hundred milliseconds;
- shutdown of a part of the network, the extent of that part depending on the design of the network and the discrimination levels offered by the protection devices;
- dynamic instability and/or the loss of machine synchronisation;
- disturbances in control / monitoring circuits,
- etc...

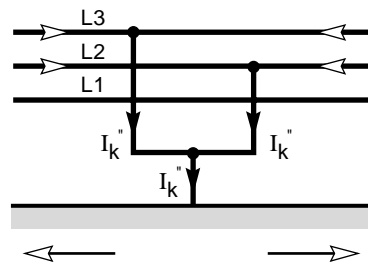
a) Symmetrical three-phase short-circuit.



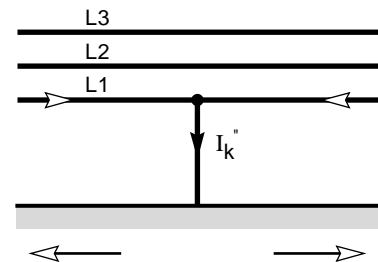
b) Phase-to-phase short-circuit clear of earth.



c) Phase-to-phase-to-earth short-circuit.



d) Phase-earth short-circuit.



- Short-circuit current,
- Partial short-circuit currents in conductors and earth.

In calculations, the various currents (I_k'') are identified by an index.

Fig. 5: different types of short-circuits and their currents. The direction of current is chosen arbitrarily. (See IEC 60909).

1.2 Establishing the short-circuit current

A simplified network comprises a source of constant AC power, a switch, an impedance Z_{sc} that represents all the impedances upstream of the switch, and a load impedance Z_s (see **fig. 6**).

In a real network, the source impedance is made up of everything upstream of the short-circuit including the various networks with different voltages (HV, LV) and the series-connected wiring systems with different cross-sectional areas (A) and lengths.

In **figure 6**, when the switch is closed, the design current I_s flows through the network.

When a fault occurs between A and B, the negligible impedance between these points results in a very high short-circuit current I_{sc} that is limited only by impedance Z_{sc} .

The current I_{sc} develops under transient conditions depending on the reactances X and the resistances R that make up impedance Z_{sc} :

$$Z_{sc} = \sqrt{R^2 + X^2}$$

In power distribution networks, reactance $X = L \omega$ is normally much greater than resistance

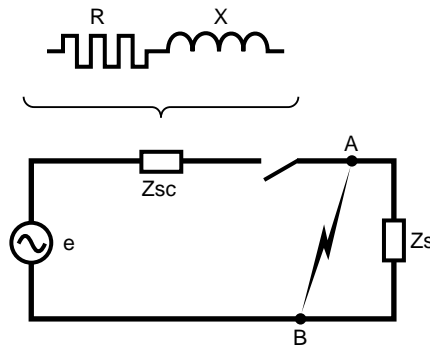


Fig. 6: simplified network diagram.

R and the R / X ratio is between 0.1 and 0.3. The ratio is virtually equal to $\cos \varphi_{sc}$ for low values:

$$\cos \varphi_{sc} = \frac{R}{\sqrt{R^2 + X^2}}$$

However, the transient conditions prevailing while the short-circuit current develops differ depending on the distance between the fault location and the generator. This distance is not necessarily physical, but means that the generator impedances are less than the link impedance between the generator and the fault location.

Fault away from the generator

This is the most frequent situation. The transient conditions are those resulting from the application of a voltage to a reactor-resistance circuit. This voltage is:

$$e = E \sin(\omega t + \alpha)$$

Current i is then the sum of the two components:

$$i = i_a + i_{dc}$$

■ The first (i_a) is alternating and sinusoidal:

$$i_a = I \sin(\omega t + \alpha) \text{ where}$$

$$I = \text{maximum current} = \frac{E}{Z_{sc}}$$

α = angle characterising the difference between the initiation of the fault and zero voltage.

■ The second (i_{dc}) is an aperiodic component,

$$i_{dc} = -I \sin \alpha e^{-\frac{R}{L} t}$$

Its initial value depends on α and its decay rate is proportional to R / L .

At the initiation of the short-circuit, i is equal to zero by definition (the design current I_s is negligible), hence:

$$i = i_a + i_{dc} = 0$$

Figure 7 shows the graphical composition of i as the algebraic sum of its two components i_a et i_{dc} .

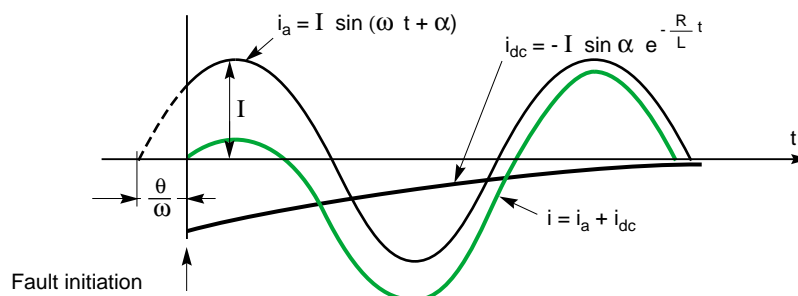
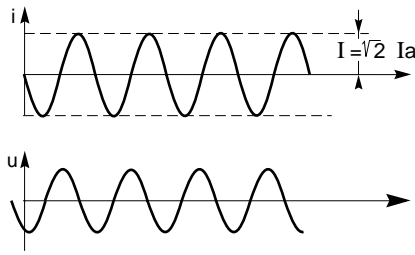


Fig. 7: graphical presentation and decomposition of a short-circuit current occurring away from the generator.

a) Symmetrical



b) Asymmetrical

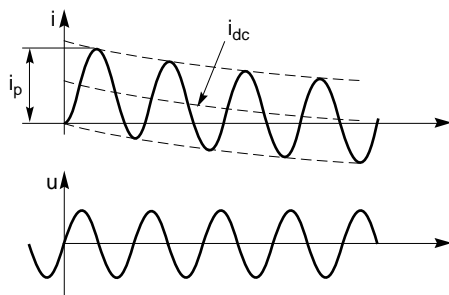


Fig. 8: graphical presentation of the two extreme cases (symmetrical and asymmetrical) for a short-circuit current.

Figure 8 illustrates the two extreme cases for the development of a short-circuit current, presented, for the sake of simplicity, with a single-phase, alternating voltage.

The factor $e^{-\frac{R}{L}t}$ is inversely proportional to the aperiodic component damping, determined by the R/L or R/X ratios.

The value of i_p must therefore be calculated to determine the making capacity of the required circuit breakers and to define the electrodynamic forces that the installation as a whole must be capable of withstanding.

Its value may be deduced from the rms value of the symmetrical short-circuit current I_a using the equation:

$i_p = K \sqrt{2} I_a$ where the coefficient K is indicated by the curve in figure 9, as a function of the ratio R/X or R/L .

Fault near the generator

When the fault occurs in the immediate vicinity of the generator supplying the circuit, the variation in the impedance of the generator, in this case the dominant impedance, damps the short-circuit current.

The transient current-development conditions are complicated by the variation in the electromotive force resulting from the short-circuit. For simplicity, the electromotive force is

assumed to be constant and the internal reactance of the machine variable. The reactance develops in three stages:

$$i = \frac{E}{Z} \left[\sin(\omega t + \alpha - \varphi) - \sin(\alpha - \varphi) e^{-\frac{R}{L}t} \right]$$

with its two components, one being alternating with a shift equal to φ with respect to the voltage and the second aperiodic and decaying to zero as t tends to infinity. Hence the two extreme cases defined by:

■ $\alpha = \varphi \approx \pi/2$, said to be symmetrical (or balanced), (see figure a).

The fault current can be defined by: $i = \frac{E}{Z} \sin \omega t$ which, from the initiation, has the same shape as for steady state conditions with a peak value E/Z .

■ $\alpha = 0$, said to be asymmetrical (or unbalanced), (see figure b).

The fault current can be defined by:

$$i = \frac{E}{Z} \left[\sin(\omega t - \varphi) - \sin \varphi e^{-\frac{R}{L}t} \right]$$

Its initial peak value i_p therefore depends on φ , i.e. on the $R/X = \cos \varphi$ ratio of the circuit.

assumed to be constant and the internal reactance of the machine variable. The reactance develops in three stages:

■ **subtransient** (the first 10 to 20 milliseconds of the fault);

■ **transient** (up to 500 milliseconds);

■ **steady-state** (or synchronous reactance).

Note that in the indicated order, the reactance acquires a higher value at each stage, i.e. the subtransient reactance is less than the transient reactance, itself less than the steady-state reactance. The successive effect of the three reactances leads to a gradual reduction in the

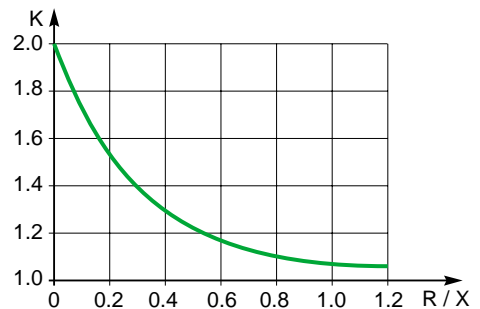


Fig. 9: variation of coefficient K depending on R/X or R/L (see IEC 60909).

short-circuit current which is the sum of four components (see **fig. 10**):

- the three alternating components (subtransient, transient and steady-state);
- the aperiodic component resulting from the development of the current in the circuit (inductive).

Practically speaking, information on the development of the short-circuit current is not essential:

- in a LV installation, due to the speed of the breaking devices, the value of the subtransient short-circuit current, denoted I_k'' , and of the maximum asymmetrical peak amplitude i_p is

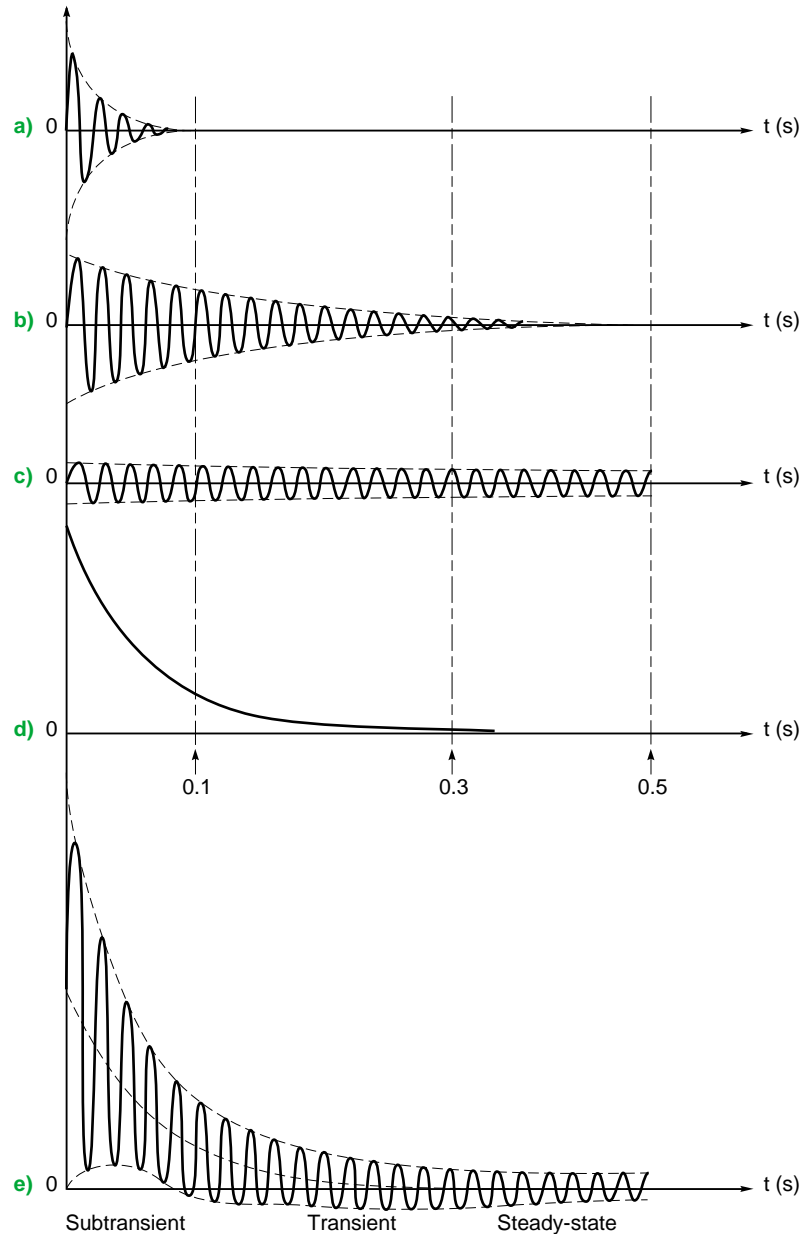


Fig. 10: total short-circuit current I_{sc} (e), and contribution of its components:

- a) subtransient of each reactance;
- b) transient reactance;
- c) steady-state reactance;
- d) aperiodic component.

Note that the decrease in the generator reactance is faster than that of the aperiodic component. This is a rare situation that can cause saturation of the magnetic circuits and interruption problems because several periods occur before the current passes through zero.

sufficient when determining the breaking capacities of the protection devices and the electrodynamic forces;

■ in LV power distribution and in HV applications, however, the transient short-circuit current is often used if breaking occurs before the steady-state stage, in which case it becomes useful to use the short-circuit breaking current, denoted I_b , which determines the breaking capacity of the time-delayed circuit breakers. I_b is the value of the short-circuit current at the moment

interruption is effective, i.e. following a time t after the development of the short-circuit, where $t = t_{min}$. Time t_{min} (minimum time delay) is the sum of the minimum operating time of a protection relay and the shortest opening time of the associated circuit breaker, i.e. the shortest time between the appearance of the short-circuit current and the initial separation of the pole contacts on the switching device.

Figure 11 presents the various currents of the short-circuits defined above.

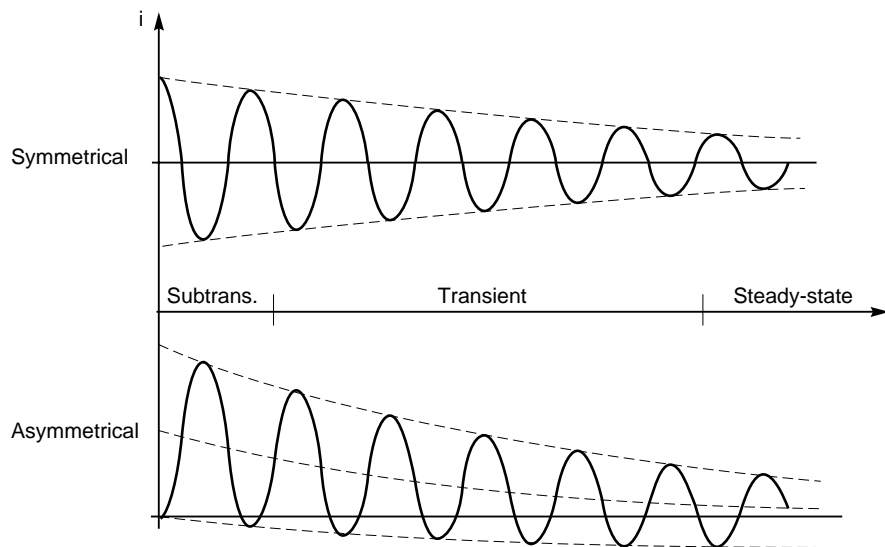


Fig. 11: short-circuit currents near a generator (schematic diagram).

1.3 Standardised I_{sc} calculations

The standards propose a number of method.

■ Application guide C 15-105, which supplements NF C 15-100 (Normes Françaises) (low-voltage AC installations), details four methods:

□ the "impedance" method, used to calculate fault currents at any point in an installation with a high degree of accuracy.

This method involves adding the various resistances and reactances of the fault loop separately, from (and including) the source to the given point, and then calculating the corresponding impedance. The I_{sc} value is finally obtained by applying Ohm's law:

$$I_{sc} = U_n / \sum(Z)$$

All the characteristics of the various elements in the fault loop must be known (sources and wiring systems).

Note that in the application guide, a number of factors are not taken into account, notably:

- the reactances of the circuit breakers and the busbars;
- the resistances of rotating machines.

The results obtained may be different from those presented in the next chapter, because these factors are taken into account;

□ the "composition" method, which may be used when the characteristics of the power supply are not known. The upstream impedance of the given circuit is calculated on the basis of an estimate of the short-circuit current at its origin. Power factor $\cos \phi_{sc} = R / X$ is assumed to be identical at the origin of the circuit and the fault location. In other words, it is assumed that the elementary impedances of two successive sections in the installation are sufficiently similar in their characteristics to justify the replacement of vectorial addition of the impedances by algebraic addition. This approximation may be used to calculate the value of the short-circuit current modulus with sufficient accuracy for the addition of a circuit. This very approximate method should be used only for installations rated up to 800 kVA;

□ the "conventional" method, which can be used, when the impedances or the I_{sc} in the installation upstream of the given circuit are not

known, to calculate the minimum short-circuit currents and the fault currents at the end of a line. It is based on the assumption that the voltage at the circuit origin is equal to 80 % of the rated voltage of the installation during the short-circuit or the fault.

This method considers only the resistance of the conductors and applies a coefficient greater than 1 to conductors with large cross-sectional areas to take into account their inductance (1.15 for 150 mm², 1.20 for 185 mm², etc.). It is mainly used for final circuits with their origin at a distance that is sufficiently far from the power source (network or power-station unit);

□ the "simplified" method (presented in detail in this application guide), which, via tables based on numerous simplifying assumptions, indicates for each conductor cross-sectional area:

- the current rating of the overload protection device;
- maximum lengths of wiring systems to maintain protection against indirect contact;
- permissible lengths in view of line voltage drops.

The data in the tables is in fact the result of calculations run using essentially the

composition and conventional methods. This method may be used to determine the characteristics of a circuit to be added to an existing installation for which sufficient information is not available. It is directly applicable to LV installations, and can be used with correction coefficients if the voltage is not 230 / 400 V.

■ Standard IEC 909 (VDE 0102) applies to all networks, radial or meshed, up to 230 kV. This method, based on the Thevenin theorem, calculates an equivalent voltage source at the short-circuit location and then determines the corresponding short-circuit current. All network feeders as well as the synchronous and asynchronous machines are replaced in the calculation by their impedances (positive sequence, negative-sequence and zero-sequence). All line capacitances and the parallel admittances of non-rotating loads, except those of the zero-sequence system, are neglected.

■ Other methods use the superposition principle and require that the load current first be calculated. Note also the method proposed by standard IEC 865 (VDE 0103) which calculates the thermally equivalent short-circuit current.

1.4 Methods presented in this document

In this "Cahier Technique" publication, two methods are presented for the calculation of short-circuit currents in radial networks:

■ the impedance method, reserved primarily for LV networks, was selected for its high degree of accuracy and its instructive value, given that virtually all characteristics of the circuit are taken into account.

■ the IEC 60909 method, used primarily for HV networks, was selected for its accuracy and its analytical character. More technical in nature, it implements the symmetrical-component principle.

1.5 Basic assumptions

To simplify the short-circuit calculations, a number of assumptions are required. These impose limits for which the calculations are valid but usually provide good approximations, facilitating comprehension of the physical phenomena and consequently the short-circuit current calculations. They nevertheless maintain a fully acceptable level of accuracy, "erring" systematically on the conservative side. The assumptions used in this document are as follows:

- the given network is radial with rated voltages ranging from LV to HV, but not exceeding 230 kV, the limit set by standard IEC 60909;
- the short-circuit current, during a three-phase short-circuit, is assumed to occur simultaneously on all three phases;
- during the short-circuit, the number of phases involved does not change, i.e. a three-phase

fault remains three-phase and a phase-to-earth fault remains phase-to-earth;

- for the entire duration of the short-circuit, the voltages responsible for the flow of the current and the short-circuit impedance do not change significantly;
- transformer regulators or tap-changers are assumed to be set to a medium position (if the short-circuit occurs away from the generator, the actual position of the transformer regulator or tap-changers does not need to be taken into account);
- arc resistances are not taken into account;
- all line capacitances are neglected;
- load currents are neglected;
- all zero-sequence impedances are taken into account.

2 Calculation of Isc by the impedance method

2.1 Isc depending on the different types of short-circuit

Three-phase short-circuit

This fault involves all three phases. Short-circuit current I_{sc3} is equal to:

$$I_{sc3} = \frac{U / \sqrt{3}}{Z_{sc}}$$

where U (phase-to-phase voltage) corresponds to the transformer no-load voltage which is 3 to 5 % greater than the on-load voltage across the terminals. For example, in 390 V networks, the phase-to-phase voltage adopted is $U = 410$, and the phase-to-neutral voltage is $U / \sqrt{3} = 237$ V. Calculation of the short-circuit current therefore requires only calculation of Z_{sc} , the impedance equal to all the impedances through which I_{sc}

flows from the generator to the location of the fault, i.e. the impedances of the power sources and the lines (see **fig. 12**). This is, in fact, the "positive-sequence" impedance per phase:

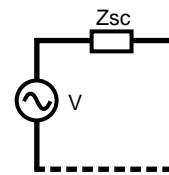
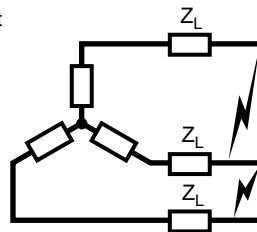
$$Z_{sc} = \sqrt{(\sum R)^2 + (\sum X)^2} \text{ where}$$

$\sum R$ = the sum of series resistances,

$\sum X$ = the sum of series reactances.

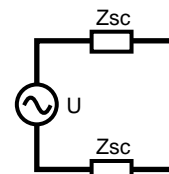
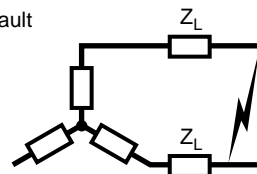
It is generally considered that three-phase faults provoke the highest fault currents. The fault current in an equivalent diagram of a polyphase system is limited by only the impedance of one phase at the phase-to-neutral voltage of the

Three-phase fault



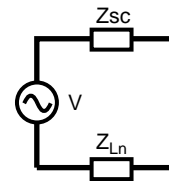
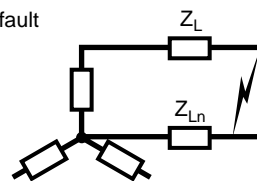
$$I_{sc3} = \frac{U / \sqrt{3}}{Z_{sc}}$$

Phase-to-phase fault



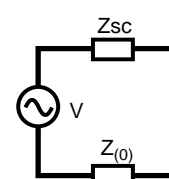
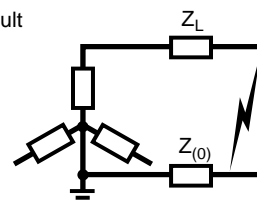
$$I_{sc2} = \frac{U}{2 Z_{sc}}$$

Phase-to-neutral fault



$$I_{sc1} = \frac{U / \sqrt{3}}{Z_{sc} + Z_{Ln}}$$

Phase-to-earth fault



$$I_{sc(0)} = \frac{U / \sqrt{3}}{Z_{sc} + Z_{(0)}}$$

Fig. 12: the various short-circuit currents.

network. Calculation of I_{sc3} is therefore essential for selection of equipment (maximum current and electrodynamic withstand capability).

Phase-to-phase short-circuit clear of earth

This is a fault between two phases, supplied with a phase-to-phase voltage U .

In this case, the short-circuit current I_{sc2} is less than that of a three-phase fault:

$$I_{sc2} = \frac{U}{2 Z_{sc}} = \frac{\sqrt{3}}{2} I_{sc3} \approx 0.86 I_{sc3}$$

Phase-to-neutral short-circuit clear of earth

This is a fault between one phase and the neutral, supplied with a phase-to-neutral voltage $V = U / \sqrt{3}$.

The short-circuit current I_{sc1} is:

$$I_{sc1} = \frac{U / \sqrt{3}}{Z_{sc} + Z_{Ln}}$$

In certain special cases of phase-to-neutral faults, the zero-sequence impedance of the

source is less than Z_{sc} (for example, at the terminals of a star-zigzag connected transformer or of a generator under subtransient conditions). In this case, the phase-to-neutral fault current may be greater than that of a three-phase fault.

Phase-to-earth fault (one or two phases)

This type of fault brings the zero-sequence impedance $Z_{(0)}$ into play.

Except when rotating machines are involved (reduced zero-sequence impedance), the short-circuit current $I_{sc(0)}$ is less than that of a three-phase fault.

Calculation of $I_{sc(0)}$ may be necessary, depending on the neutral system (system earthing arrangement), in view of defining the setting thresholds for the zero-sequence (HV) or earth-fault (LV) protection devices.

Figure 12 shows the various short-circuit currents

2.2 Determining the various short-circuit impedances

This method involves determining the short-circuit currents on the basis of the impedance represented by the "circuit" through which the short-circuit current flows. This impedance may be calculated after separately summing the various resistances and reactances in the fault loop, from (and including) the power source to the fault location.

(The circled numbers (X) may be used to come back to important information while reading the example at the end of this section.)

Network impedances

■ Upstream network impedance

Generally speaking, points upstream of the power source are not taken into account. Available data on the upstream network is therefore limited to that supplied by the power distributor, i.e. only the short-circuit power S_{sc} in MVA.

The equivalent impedance of the upstream network is:

$$(1) Z_{up} = \frac{U^2}{S_{sc}}$$

where U is the no-load phase-to-phase voltage of the network.

The upstream resistance and reactance may be deduced from R_{up} / Z_{up} (for HV) by:

$R_{up} / Z_{up} \approx 0.3$ at 6 kV;
 $R_{up} / Z_{up} \approx 0.2$ at 20 kV;
 $R_{up} / Z_{up} \approx 0.1$ at 150 kV.

$$As, X_{up} = \sqrt{Z_{up}^2 - R_{up}^2},$$

$$\frac{X_{up}}{Z_{up}} = \sqrt{1 - \left(\frac{R_{up}}{Z_{up}}\right)^2}$$

(2) Therefore, for 20 kV,

$$\frac{X_{up}}{Z_{up}} = \sqrt{1 - (0,2)^2} = 0,980$$

$X_{up} = 0.980 Z_{up}$ at 20 kV,
hence the approximation $X_{up} \approx Z_{up}$.

■ Internal transformer impedance

The impedance may be calculated on the basis of the short-circuit voltage u_{sc} expressed as a percentage:

$$(3) Z_T = u_{sc} \frac{U^2}{S_n} \text{ where}$$

U = no-load phase-to-phase voltage of the transformer;

S_n = transformer kVA rating;

$U u_{sc}$ = voltage that must be applied to the primary winding of the transformer for the rated current to flow through the secondary winding, when the LV secondary terminals are short-circuited.

For public distribution MV / LV transformers, the values of u_{sc} have been set by the European Harmonisation document HD 428-1S1 issued in October 1992 (see **fig. 13**).

Rating (kVA) of the HV / LV transformer	≤ 630	800	1,000	1,250	1,600	2,000
Short-circuit voltage u_{sc} (%)	4	4.5	5	5.5	6	7

Fig. 13: standardised short-circuit voltage for public distribution transformers.

Note that the accuracy of values has a direct influence on the calculation of I_{sc} in that an error of $x\%$ for u_{sc} produces an equivalent error ($x\%$) for Z_T .

④ In general, $R_T \ll X_T$, in the order of $0.2 X_T$, and the internal transformer impedance may be considered comparable to reactance X_T . For low power levels, however, calculation of Z_T is required because the ratio R_T / X_T is higher. The resistance is calculated using the joule losses (W) in the windings:

$$W = 3 R_T I_n^2 \Rightarrow R_T = \frac{W}{3 I_n^2}$$

Notes:

⑤

□ when n identically-rated transformers are connected in parallel, their internal impedance values, as well as the resistance and reactance values, must be divided by n .

□ particular attention must be paid to special transformers, for example, the transformers for rectifier units have u_{sc} values of up to 10 to 12 % in order to limit short-circuit currents.

When the impedance upstream of the transformer and the transformer internal impedance are taken into account, the short-circuit current may be expressed as:

$$I_{sc} = \frac{U}{\sqrt{3}(Z_{up} + Z_T)}$$

Initially, Z_{up} and Z_T may be considered comparable to their respective reactances. The short-circuit impedance Z_{sc} is therefore equal to the algebraic sum of the two.

The upstream network impedance may be neglected, in which case the new current value is:

$$I'_{sc} = \frac{U}{\sqrt{3} Z_T}$$

The relative error is:

$$\frac{\Delta I_{sc}}{I_{sc}} = \frac{I'_{sc} - I_{sc}}{I_{sc}} = \frac{Z_{up}}{Z_T} = \frac{U^2 / S_{sc}}{u_{sc} U^2 / S_n}$$

i.e.:

$$\frac{\Delta I_{sc}}{I_{sc}} = \frac{100}{u_{sc}} \frac{S_n}{S_{sc}}$$

Figure 14 indicates the level of conservative error in the calculation of I_{sc} , due to the fact that the upstream impedance is neglected. The figure demonstrates clearly that it is possible to neglect the upstream impedance for networks where the short-circuit power S_{sc} is much higher than the transformer kVA rating S_n . For example, when $S_{sc} / S_n = 300$, the error is approximately 5 %.

■ Link impedance

The link impedance Z_L depends on the resistance per unit length, the reactance per unit length and the length of the links.

□ the resistance per unit length of overhead lines, cables and busbars is calculated as:

$$R_L = \frac{\rho}{A}$$

where

A = cross-sectional area of the conductor;
 ρ = conductor resistivity, however the value used varies, depending on the calculated short-circuit current (minimum or maximum).

⑥ The table in figure 15 provides values for each of the above-mentioned cases.

Practically speaking, for LV and conductors with cross-sectional areas less than 150 mm^2 , only the resistance is taken into account ($R_L < 0.15 \text{ m}\Omega / \text{m}$ when $A > 150 \text{ mm}^2$).

□ the reactance per unit length of overhead lines, cables and busbars may be calculated as:

$$X_L = L \omega = \left[15.7 + 144.44 \text{ Log} \left(\frac{d}{r} \right) \right]$$

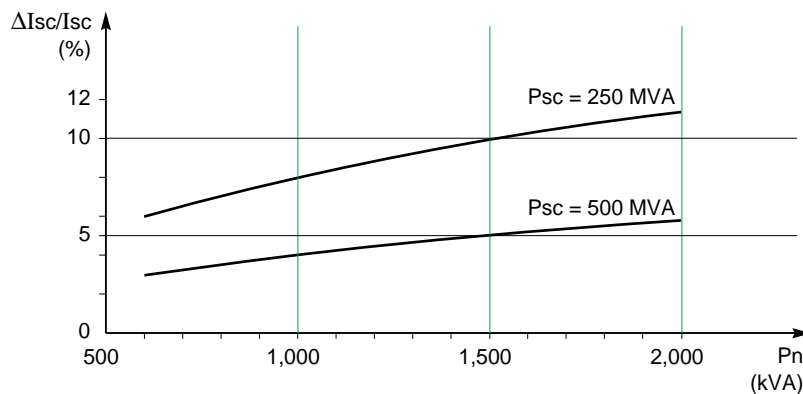


Fig. 14 : resultant error in the calculation of the short-circuit current when the upstream network impedance Z_{up} is neglected.

expressed as $m\Omega / km$ for a single-phase or three-phase delta cable system, where (in mm):
 r = radius of the conducting cores;
 d = average distance between conductors.

N.B. Above, Log = decimal logarithm.

For overhead lines, the reactance increases slightly in proportion to the distance between conductors ($\text{Log} \left(\frac{d}{t} \right)$), and therefore in proportion to the operating voltage.

⑦ the following average values are to be used:

$X = 0.3 \Omega / km$ (LV lines);

$X = 0.4 \Omega / km$ (MV or HV lines).

The table in **figure 16** shows the various reactance values for conductors in LV applications, depending on the wiring system. The following average values are to be used:

- $0.08 m\Omega / m$ for a three-phase cable (③),
 and, for HV applications, between 0.1 and $0.15 m\Omega / m$.

⑧ - $0.09 m\Omega / m$ for touching, single-conductor cables (flat ②②② or triangular ③③);

⑨ - $0.15 m\Omega / m$ as a typical value for busbars

(④④④) and spaced, single-conductor cables

(①①①); For "sandwiched-phase" busbars (e.g. Canalis - Telemecanique), the reactance is considerably lower.

Notes:

□ the impedance of the short links between the distribution point and the HV / LV transformer may be neglected. This assumption gives a conservative error concerning the short-circuit current. The error increases in proportion to the transformer rating.

□ the cable capacitance with respect to the earth (common mode), which is 10 to 20 times greater than that between the lines, must be taken into account for earth faults. Generally speaking, the

Current	Resistivity (*)	Resistivity value ($\Omega mm^2 / m$)		Concerned conductors
		Copper	Aluminium	
Maximum short-circuit current	$\rho_1 = 1.25 \rho_{20}$	0.0225	0.036	PH-N
Minimum short-circuit current	$\rho_1 = 1.5 \rho_{20}$	0.027	0.043	PH-N
Fault current in TN and IT systems	$\rho_1 = 1.25 \rho_{20}$	0.0225	0.036	PH-N (**) PE-PEN
Voltage drop	$\rho_1 = 1.25 \rho_{20}$	0.0225	0.036	PH-N (**)
Overcurrent for conductor thermal-stress checks	$\rho_1 = 1.5 \rho_{20}$	0.027	0.043	Phase-Neutral PEN-PE if incorporated in same multiconductor cable
	$\rho_1 = 1.25 \rho_{20}$	0.0225	0.036	Separate PE

(*) ρ_{20} is the resistivity of the conductors at $20^\circ C$. $0.018 \Omega mm^2 / m$ for copper and $0.029 \Omega mm^2 / m$ for aluminium.
 (**) N, the cross-sectional area of the neutral conductor, is less than that of the phase conductor

Fig. 15: conductor resistivity ρ values to be taken into account depending on the calculated short-circuit current (minimum or maximum). See UTE C 15-105.






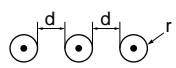
Wiring system	Busbars	Three-phase cable	Spaced single-core espacés	Touching single-core cables (triangle)	3 touching cables (flat)	3 "d" spaced cables (flat) $d = 2r$ $d = 4r$	
Diagram							
Average reactance per unit length values ($m\Omega / m$)	0.15	0.08	0.15	0.085	0.095	0.145	0.19
Extreme reactance per unit length values ($m\Omega / m$)	0.12-0.18	0.06-0.1	0.1-0.2	0.08-0.09	0.09-0.1	0.14-0.15	0.18-0.20

Fig. 16: cables reactance values depending on the wiring system.

capacitance of a HV three-phase cable with a cross-sectional area of 120 mm² is in the order of 1 μF / km, however the capacitive current remains low, in the order of 5 A / km at 20 kV.

■ The reactance or resistance of the links may be neglected.
If one of the values, R_L or X_L, is low with respect to the other, it may be neglected because the resulting error for impedance Z_L is consequently very low. For example, if the ratio between R_L and X_L is 3, the error in Z_L is 5.1 %.

The curves for R_L and X_L (see fig. 17) may be used to deduce the cable cross-sectional areas for which the impedance may be considered comparable to the resistance or to the reactance.

Examples:

□ first case. Consider a three-phase cable, at 20 °C, with **copper** conductors. Their reactance is 0.08 mΩ / m. The R_L and X_L curves (see fig. 17) indicate that impedance Z_L approaches two asymptotes, R_L for low cable cross-sectional areas and X_L = 0.08 mΩ / m for high cable cross-sectional areas. For the low and high cable cross-sectional areas, the impedance Z_L curve may be considered identical to the asymptotes.

The given cable impedance is therefore considered, with a margin of error less than 5.1 %, comparable to:

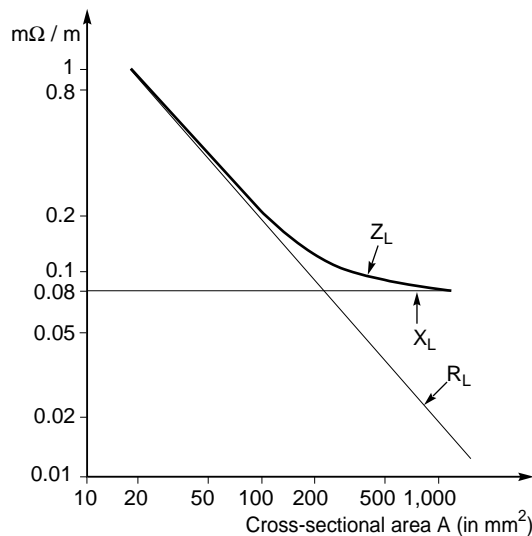


Fig. 17: impedance Z_L of a three-phase cable, at 20 °C, with copper conductors.

- a resistance for cable cross-sectional areas less than 74 mm²;
- a reactance for cable cross-sectional areas greater than 660 mm².

□ second case. Consider a three-phase cable, at 20 °C, with aluminium conductors. As above, the impedance Z_L curve may be considered identical to the asymptotes, but for cable cross-sectional areas less than 120 mm² and greater than 1,000 mm² (curves not shown).

Impedance of rotating machines

■ Synchronous generators

The impedances of machines are generally expressed as a percentage, for example: I_{sc} / I_n = 100 / x where x is the equivalent of the transformer u_{sc}.

Consider:

$$(10) Z = \frac{x}{100} \frac{U^2}{S_n} \text{ where}$$

U = no-load phase-to-phase voltage of the generator,

S_n = generator VA rating.

(11) What is more, given that the value of R / X is low, in the order of 0.05 to 0.1 for MV and 0.1 to 0.2 for LV, impedance Z may be considered comparable to reactance X. Values for x are given in the table in figure 18 for turbo-generators with smooth rotors and for "hydraulic" generators with salient poles (low speeds).

On reading the table, one may be surprised to note that the steady-state reactance for a short-circuit exceeds 100 % (at that point in time, I_{sc} < I_n). However, the short-circuit current is essentially inductive and calls on all the reactive power that the field system, even over-excited, can supply, whereas the rated current essentially carries the active power supplied by the turbine (cos φ from 0.8 to 1).

■ Synchronous compensators and motors

The reaction of these machines during a short-circuit is similar to that of generators.

(12) They produce a current in the network that depends on their reactance in % (see fig. 19).

■ Asynchronous motors

When an asynchronous motor is cut from the network, it maintains a voltage across its terminals that disappears within a few

	Subtransient reactance	Transient reactance	Steady-state reactance
Turbo-generator	10-20	15-25	150-230
Salient-pole generators	15-25	25-35	70-120

Fig. 18: generator reactance values, in x %.

	Subtransient reactance	Transient reactance	Steady-state reactance
High-speed motors	15	25	80
Low-speed motors	35	50	100
Compensators	25	40	160

Fig. 19: synchronous compensator and motor reactance values, in x %.

hundredths of a second. When a short-circuit occurs across the terminals, the motor supplies a current that disappears even more rapidly, according to time constants in the order of:

- 0.02 seconds for single-cage motors up to 100 kW;
- 0.03 seconds for double-cage motors and motors above 100 kW;
- 0.03 to 0.1 seconds for very large HV slipping motors (1,000 kW).

In the event of a short-circuit, an asynchronous motor is therefore a generator to which an impedance (subtransient only) of 20 to 25 % is attributed.

Consequently, the large number of LV motors, with low individual outputs, present on industrial sites may be a source of difficulties in that it is not easy to foresee the average number of in-service motors that will contribute to the fault when a short-circuit occurs. Individual calculation of the reverse current for each motor, taking into account the impedance of its link, is therefore a tedious and futile task. Common practice, notably in the United States, is to take into account the combined contribution to the fault current of all the asynchronous LV motors in an installation.

⑬ They are therefore thought of as a unique source, capable of supplying to the busbars a current equal to (I_{start} / I_n) times the sum of the rated currents of all installed motors.

Other impedances

■ Capacitors

A shunt capacitor bank located near the fault location discharges, thus increasing the short-circuit current. This damped oscillatory discharge is characterised by a high initial peak value that is superposed on the initial peak of the short-circuit current, even though its frequency is far greater than that of the network.

Depending on the coincidence in time between the initiation of the fault and the voltage wave, two extreme cases must be considered:

- if the initiation of the fault coincides with zero voltage, the discharge current is equal to zero, whereas the short-circuit current is asymmetrical, with a maximum initial amplitude peak;
- conversely, if the initiation of the fault coincides with maximum voltage, the discharge current superposes itself on the initial peak of the fault current, which, because it is symmetrical, has a low value.

It is therefore unlikely, except for very powerful capacitor banks, that superposition will result in an initial peak higher than the peak current of an asymmetrical fault.

It follows that when calculating the maximum short-circuit current, capacitor banks do not need to be taken into account.

However, they must nonetheless be considered when selecting the type of circuit breaker. During opening, capacitor banks significantly reduce the circuit frequency and thus produce an effect on current interruption.

■ Switchgear

⑭ Certain devices (circuit breakers, contactors with blow-out coils, direct thermal relays, etc.) have an impedance that must be taken into account, for the calculation of I_{sc} , when such a device is located upstream of the device intended to break the given short-circuit and remain closed (selective circuit breakers).

⑮ For LV circuit breakers, for example, a reactance value of 0.15 mΩ is typical, with the resistance negligible.

For breaking devices, a distinction must be made depending on the speed of opening:

- certain devices open very quickly and thus significantly reduce short-circuit currents. This is the case for fast-acting, limiting circuit breakers and the resultant level of electrodynamic forces and thermal stresses, for the part of the installation concerned, remains far below the theoretical maximum;
- other devices, such as time-delayed circuit breakers, do not offer this advantage.

■ Fault arc

The short-circuit current often flows through an arc at the fault location. The resistance of the arc is considerable and highly variable. The voltage drop over a fault arc can range from 100 to 300 V. For HV applications, this drop is negligible with respect to the network voltage and the arc has no effect on reducing the short-circuit current. For LV applications, however, the actual fault current when an arc occurs is limited to a much lower level than that calculated (bolted, solid fault), because the voltage is much lower.

⑯ For example, the arc resulting from a short-circuit between conductors or busbars may reduce the prospective short-circuit current by

20 to 50 % and sometimes by even more than 50 % for rated voltages under 440 V. However, this phenomenon, highly favourable in the LV field and which occurs for 90 % of faults, may not be taken into account when determining the breaking capacity because 10 % of faults take place during closing of a device, producing a solid fault without an arc. This phenomenon should, however, be taken into account for the calculation of the minimum short-circuit current.

■ Various impedances
Other elements may add non-negligible impedances. This is the case for harmonics filters and inductors used to limit the short-circuit current. They must, of course, be included in calculations, as well as wound-primary type current transformers for which the impedance values vary depending on the rating and the type of construction.

2.3 Relationships between impedances at the different voltage levels in an installation

Impedances as a function of the voltage

The short-circuit power S_{sc} at a given point in the network is defined by:

$$S_{sc} = U I \sqrt{3} = \frac{U^2}{Z_{sc}}$$

This means of expressing the short-circuit power implies that S_{sc} is invariable at a given point in the network, whatever the voltage. And the

equation $I_{sc3} = \frac{U}{\sqrt{3} Z_{sc}}$ implies that all

impedances must be calculated with respect to the voltage at the fault location, which leads to certain complications that often produce errors in calculations for networks with two or more voltage levels. For example, the impedance of a HV line must be multiplied by the square of the reciprocal of the transformation ratio, when calculating a fault on the LV side of the transformer:

$$(17) Z_{LV} = Z_{HV} \left(\frac{U_{LV}}{U_{HV}} \right)^2$$

A simple means of avoiding these difficulties is the relative impedance method proposed by H. Rich.

Calculation of the relative impedances

This is a calculation method used to establish a relationship between the impedances at the different voltage levels in an electrical installation.

This method proposes dividing the impedances (in ohms) by the square of the network line-to-line voltage (in volts) at the point where the impedances exist. The impedances therefore become relative.

■ For lines and cables, the relative resistances and reactances are defined as:

$$R_R = \frac{R}{U^2} \text{ and } X_R = \frac{X}{U^2} \text{ where } R \text{ is in ohms and } U \text{ in volts.}$$

■ For transformers, the impedance is expressed on the basis of their short-circuit voltages u_{sc} and their kVA rating S_n :

$$Z = \frac{U^2}{S_n} \frac{u_{sc}}{100}$$

■ For rotating machines, the equation is identical, with x representing the impedance expressed in %.

■ For the system as a whole, after having calculated all the relative impedances, the short-circuit power may be expressed as:

$S_{sc} = \frac{1}{\sum Z_R}$ from which it is possible to deduce the fault current I_{sc} at a point with a voltage U :

$$I_{sc} = \frac{S_{sc}}{\sqrt{3} U} = \frac{1}{\sqrt{3} U \sum Z_R}$$

$\sum Z_R$ is the composed vector sum of all the relative upstream impedances. It is therefore the relative impedance of the upstream network as seen from a point at U voltage.

Hence, S_{sc} is the short-circuit power, in VA, at a point where voltage is U .

For example, if we consider the simplified diagram of **figure 20** :

$$\text{At point A, } S_{sc} = \frac{U_{LV}^2}{Z_T \left(\frac{U_{LV}}{U_{HV}} \right)^2 + Z_L}$$

$$\text{Hence, } S_{sc} = \frac{1}{\frac{Z_T}{U_{HV}^2} + \frac{Z_L}{U_{LV}^2}}$$

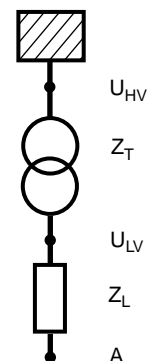


Fig. 20: calculating S_{sc} at point A.

2.4 Calculation example

(with the impedances of the power sources, the upstream network and the power supply transformers as well as those of the electrical links)

Problem

Consider a 20 kV network that supplies a HV / LV substation via a 2 km overhead line, and a 1 MVA generator that supplies in parallel the busbars of the same substation. Two 1,000 kVA parallel-connected transformers supply the LV busbars which in turn supply 20 outgoers to 20 motors, including the one supplying motor M. All motors are rated 50 kW, all connection cables

are identical and all motors are running when the fault occurs.

The I_{sc} value must be calculated at the various fault locations indicated in the network diagram (see [fig. 21](#)), that is:

- point A on the HV busbars, with a negligible impedance;
- point B on the LV busbars, at a distance of 10 meters from the transformers;
- point C on the busbars of an LV sub-distribution board;
- point D at the terminals of motor M.

Then the reverse current of the motors must be calculated at C and B, then at D and A.

Upstream network

$U_1 = 20$ kV

$P_{sc} = 500$ MVA

Overhead line

3 cables, 50 mm², copper, length = 2 km

Generator

1 MVA

$X_{subt} = 15$ %

2 transformers

1,000 kVA

secondary winding 237 / 410 V

$u_{sc} = 5$ %

Main LV switchboard

busbars

3 bars, 400 mm² / ph, copper, length = 10 m

Link 1

3 single-core cables, 400 mm², aluminium spaced, flat, length = 80 m

LV sub-distribution board

Link 2

3 three-phase cables, 35 mm², copper, length = 30 m

Motor

50 kW

(efficiency: 0.9, $\cos \varphi$: 0.8)

$u_{sc} = 25$ %

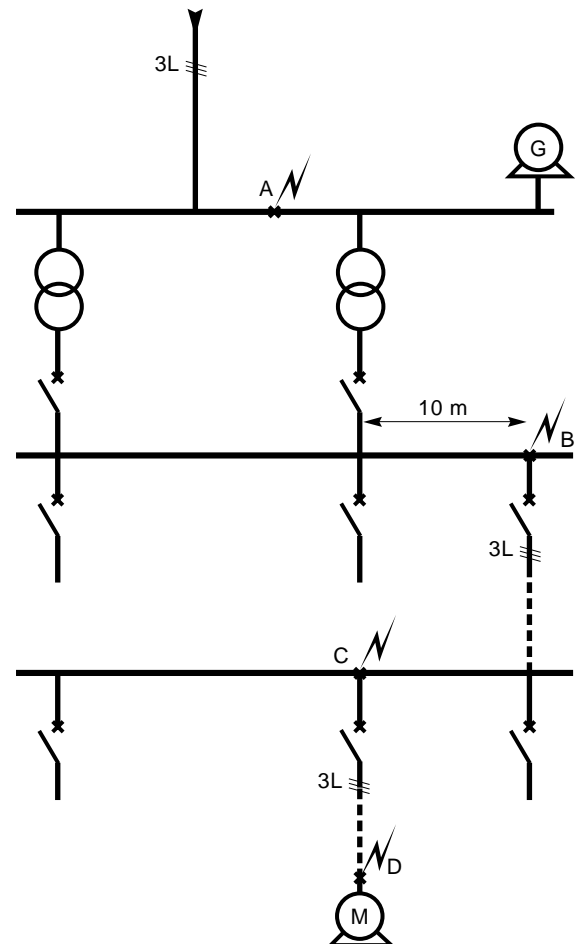


Fig. 21: diagram for calculation of I_{sc} values at points A, B, C and D.

In this example, reactances X and resistances R are calculated with their respective voltages in

the installation (see **figure 22**). The relative impedance method is not used.

Solution

Section	Calculations	Results
(the circled numbers (X) indicate where explanations may be found in the preceding text)		
20 kV↓		X (Ω) R (Ω)
1. upstream network	$Z_{up} = (20 \times 10^3)^2 / 500 \times 10^6$ (1)	
	$X_{up} = 0.98 Z_{up}$ (2)	0.78
	$R_{up} = 0.2 Z_{up} \approx 0.2 X_{up}$	0.15
2. overhead line (50 mm ²)	$X_{c_o} = 0.4 \times 2$ (7)	0.8
	$R_{c_o} = 0.018 \times \frac{2,000}{50}$ (6)	0.72
3. generator	$X_G = \frac{15}{100} \times \frac{(20 \times 10^3)^2}{10^6}$ (10)	60
	$R_G = 0.1 X_G$ (11)	6
20 kV↑ Fault A		X (mΩ) R (mΩ)
4. transformers	$Z_T = \frac{1}{2} \times \frac{5}{100} \times \frac{410^2}{10^6}$ (3) (5)	
	$X_T \approx Z_T$	4.2
	$R_T = 0.2 X_T$ (4)	0.84
410 V↓		
5. circuit-breaker	$X_{cb} = 0.15$ (15)	0.15
6. busbars (3 x 400 mm ²)	$X_B = 0.15 \times 10^{-3} \times 10$ (9)	1.5
	$R_B = 0.0225 \times \frac{10}{3 \times 400}$ (6)	≈ 0
Fault B		
7. circuit-breaker	$X_{cb} = 0.15$	0.15
8. cable link 1 (3 x 400 mm ²)	$X_{c_1} = 0.15 \times 10^{-3} \times 80$	12
	$R_{c_1} = 0.036 \times \frac{80}{3 \times 400}$ (6)	2.4
Fault C		
9. circuit-breaker	$X_{cb} = 0.15$	0.15
10. cable link 2 (35 mm ²)	$X_{c_2} = 0.09 \times 10^{-3} \times 30$ (8)	2.7
	$R_{c_2} = 0.0225 \times \frac{30}{35}$	19.2
Fault D		
11. motor 50 kW	$X_m = \frac{25}{100} \times \frac{410^2}{(50 / 0.9 \times 0.8) 10^3}$ (12)	605
	$R_m = 0.2 X_m$	121

Fig. 22: impedance calculation.

I - Fault at A (HV busbars)

Elements concerned: 1, 2, 3.

The "network + line" impedance is parallel to that of the generator, however the latter is much greater and may be neglected:

$$X_A = 0.78 + 0.8 \approx 1.58 \Omega$$

$$R_A = 0.15 + 0.72 \approx 0.87 \Omega$$

$$Z_A = \sqrt{R_A^2 + X_A^2} \approx 1.80 \Omega \text{ hence}$$

$$I_A = \frac{20 \times 10^3}{\sqrt{3} \times 1.80} \approx 6,415 \text{ A}$$

I_A is the "steady-state I_{sc} " and for the purposes of calculating the peak asymmetrical I_{sc} :

$$\frac{R_A}{X_A} = 0.55$$

hence $k = 1.2$ on the curve in figure 9 and therefore I_{sc} is equal to:

$$1.2 \times \sqrt{2} \times 6,415 = \mathbf{10,887 \text{ A}}$$

II - Fault at B (main LV switchboard busbars)

Elements concerned: (1, 2, 3) + (4, 5, 6).

The reactances X and resistances R calculated for the HV section must be recalculated for the LV network via multiplication by the square of the voltage ratio (17), i.e.:

$$(410 / 20,000)^2 = 0.42 \times 10^{-3} \text{ hence}$$

$$X_B = [(X_A \cdot 0.42) + 4.2 + 0.15 + 1.5] \cdot 10^{-3}$$

$$X_B = 6.51 \text{ m}\Omega \text{ and}$$

$$R_B = [(R_A \cdot 0.42) + 0.84] \cdot 10^{-3}$$

$$R_B = 1.2 \text{ m}\Omega$$

These calculations make clear, firstly, the low importance of the HV upstream reactance, with respect to the reactances of the two parallel transformers, and secondly, the non-negligible impedance of the 10 meter long, LV busbars.

$$Z_B = \sqrt{R_B^2 + X_B^2} = 6.62 \text{ m}\Omega \text{ hence}$$

$$I_B = \frac{410}{\sqrt{3} \times 6.62 \times 10^{-3}} \approx 35,758 \text{ A}$$

$$\frac{R_B}{X_B} = 0.18 \text{ hence } k = 1.58 \text{ on the curve in}$$

figure 9 and therefore the peak I_{sc} is equal to:

$$1.58 \times \sqrt{2} \times 35,758 = \mathbf{79,900 \text{ A}}$$

What is more, if the fault arc is taken into

account (see § ■ fault arc section (16)), I_B is

reduced to a maximum value of 28,606 A and a minimum value of 17,880 A.

III - Fault at C (busbars of LV sub-distribution board)

Elements concerned: (1, 2, 3) + (4, 5, 6) + (7, 8).

The reactances and the resistances of the circuit breaker and the cables must be added to X_B and R_B .

$$X_C = (X_B + 0.15 + 12) \cdot 10^{-3} = 18.67 \text{ m}\Omega$$

and

$$R_C = (R_B + 2.4) \cdot 10^{-3} = 3.6 \text{ m}\Omega$$

These values make clear the importance of I_{sc} limitation due to the cables.

$$Z_C = \sqrt{R_C^2 + X_C^2} \approx 19 \text{ m}\Omega$$

$$I_C = \frac{410}{\sqrt{3} \times 19 \times 10^{-3}} \approx 12,459 \text{ A}$$

$\frac{R_C}{X_C} = 0.19$ hence $k = 1.55$ on the curve in figure 9 and therefore the peak I_{sc} is equal to:

$$1.55 \times \sqrt{2} \times 12,459 \approx \mathbf{27,310 \text{ A}}$$

IV - Fault at D (LV motor)

Elements concerned:

(1, 2, 3) + (4, 5, 6) + (7, 8) + (9, 10).

The reactances and the resistances of the circuit breaker and the cables must be added to X_C and R_C .

$$X_D = (X_C + 0.15 + 2.7) \cdot 10^{-3} = 21.52 \text{ m}\Omega$$

and

$$R_D = (R_C + 19.2) \cdot 10^{-3} = 22.9 \text{ m}\Omega$$

$$Z_D = \sqrt{R_D^2 + X_D^2} \approx 31.42 \text{ m}\Omega$$

$$I_D = \frac{410}{\sqrt{3} \times 31.42 \times 10^{-3}} \approx 7,534 \text{ A}$$

$$\frac{R_D}{X_D} = 1.06 \text{ hence } k \approx 1.05 \text{ on the curve in}$$

figure 9 and therefore the peak I_{sc} is equal to:

$$1.05 \times \sqrt{2} \times 7,534 \approx \mathbf{11,187 \text{ A}}$$

As each level in the calculations makes clear, the impact of the circuit breakers is negligible compared to that of the other elements in the network.

V - Reverse currents of the motors

It is often faster to simply consider the motors as independent generators, injecting into the fault a "reverse current" that is superimposed on the network fault current.

■ Fault at C

The current produced by the motor may be calculated on the basis of the "motor + cable" impedance:

$$X_M = (605 + 2.7) \cdot 10^{-3} \approx 608 \text{ m}\Omega$$

$$R_M = (121 + 19.2) \cdot 10^{-3} \approx 140 \text{ m}\Omega$$

$$Z_M = 624 \text{ m}\Omega, \text{ hence}$$

$$I_M = \frac{410}{\sqrt{3} \times 624 \times 10^{-3}} \approx 379 \text{ A}$$

For the 20 motors

$$I_{MC} = 7,580 \text{ A.}$$

Instead of making the above calculations, it is

possible (see (13)) to estimate the current

injected by all the motors as being equal to (I_{start} / I_n) times their rated current (95 A), i.e.

$$(4.8 \times 95) \times 20 = 9,120 \text{ A.}$$

This estimate therefore allows protection by excess value with respect to I_{MC} (7,580 A).
On the basis of

$R / X = 0.3 \Rightarrow k = 1.4$ and the peak

$$I_{sc} = 1.4 \times \sqrt{2} \times 7,580 \approx \mathbf{15,005 \text{ A}}$$

Consequently, the short-circuit current (subtransient) on the LV busbars increases from 12,459 A to 20,039 A and I_{sc} from 27,310 A to 42,315 A.

■ Fault at D

The impedance to be taken into account is 1 / 19th of Z_M , plus that of the cable.

$$X_{MD} = \left(\frac{605}{19} + 2.7 \right) 10^{-3} \approx 34,5 \text{ m}\Omega$$

$$R_{MD} = \left(\frac{121}{19} + 19.2 \right) 10^{-3} \approx 25.5 \text{ m}\Omega$$

$$Z_{MD} = 43 \text{ m}\Omega \text{ hence}$$

$$I_{MD} = \frac{410}{\sqrt{3} \times 43 \times 10^{-3}} = 5,505 \text{ A}$$

giving a total at D of:
 $7,534 + 5,505 = 13,039 \text{ A rms}$, and
 $I_{sc} \approx \mathbf{20,650 \text{ A}}$.

■ Fault en B

As for the fault at C, the current produced by the motor may be calculated on the basis of the "motor + cable" impedance:

$$X_M = (605 + 2.7 + 12) 10^{-3} \approx 620 \text{ m}\Omega$$

$$R_M = (121 + 19.2 + 2.4) 10^{-3} \approx 142.6 \text{ m}\Omega$$

$$Z_M = 636 \text{ m}\Omega \text{ hence}$$

$$I_M = \frac{410}{\sqrt{3} \times 636 \times 10^{-3}} \approx 372 \text{ A}$$

For the 20 motors $I_{MB} = 7,440 \text{ A}$.

Again, it is possible to estimate the current injected by all the motors as being equal to 4.8 times their rated current (95 A), i.e. 9,120 A. The approximation again overestimates the real value of I_{MB} . Using the fact that

$R / X = 0.3 \Rightarrow k = 1.4$ and the peak

$$I_{sc} = 1.4 \sqrt{2} \times 7,440 = \mathbf{14,728 \text{ A}}$$

Consequently, the short-circuit current (subtransient) on the main LV switchboard

increases from 35,758 A to 43,198 A and the peak I_{sc} from 79,900 A to **94,628 A**.

However, as mentioned above, if the fault arc is taken into account, I_{sc} is reduced between 45.6 to 75 kA.

■ Fault at A (HV side)

Rather than calculating the equivalent impedances, it is easier to estimate (conservatively) the reverse current of the motors at A by multiplying the value at B by the

LV / HV transformation value (17), i.e.:

$$7,440 \times \frac{410}{20 \times 10^{-3}} = 152.5 \text{ A}$$

This figure, compared to the 6,415 A calculated previously, is negligible.

Rough calculation of the fault at D

This calculation makes use of all the approximations mentioned above (notably 15 and 16).

$$\sum X = 4.2 + 1.5 + 12 + 0.15$$

$$\sum X = 17.85 \text{ m}\Omega = X'_D$$

$$\sum R = 2.4 + 19.2 = 21.6 \text{ m}\Omega = R'_D$$

$$Z'_D = \sqrt{R'^2_D + X'^2_D} \approx 28.02 \text{ m}\Omega$$

$$I'_D = \frac{410}{\sqrt{3} \times 28.02 \times 10^{-3}} \approx 8,448 \text{ A}$$

hence the peak I_{sc} :

$$\sqrt{2} \times 8,448 \approx \mathbf{11,945 \text{ A}}$$

To find the peak asymmetrical I_{sc} , the above value must be increased by the contribution of the energised motors at the time of the fault (13)

i.e. 4.8 times their rated current of 95 A:

$$I_{sc} = 11,945 + (4.8 \times 95 \times \sqrt{2} \times 20) = 24,842 \text{ A}$$

Compared to the figure obtained by the full calculation (20,039), the approximate method allows a quick evaluation with an error remaining on the side of safety.

3 Calculation of Isc values in a radial network using symmetrical components

3.1 Advantages of this method

Calculation using symmetrical components is particularly useful when a three-phase network is unbalanced, because, due to magnetic phenomena, for example, the traditional "cyclical" impedances R and X are, normally speaking, no longer useable. This calculation method is also required when:

- a voltage and current system is not symmetrical (Fresnel vectors with different

moduli and imbalances exceeding 120°). This is the case for phase-to-earth or phase-to-phase short-circuits with or without earth connection;

- the network includes rotating machines and/or special transformers (Yyn connection, for example).

This method may be used for all types of radial distribution networks at all voltage levels.

3.2 Symmetrical components

Similar to the Leblanc theorem which states that a rectilinear alternating field with a sinusoidal amplitude is equivalent to two rotating fields turning in the opposite direction, the definition of symmetrical components is based on the equivalence between an unbalanced three-phase system and the sum of three balanced three-phase systems, namely the positive-sequence, negative-sequence and zero-sequence (see fig. 23).

The superposition principle may then be used to calculate the fault currents.

In the description below, the system is defined using current \vec{I}_1 as the rotation reference, where:

- $\vec{I}_{1(1)}$ is the positive-sequence component;
- $\vec{I}_{1(2)}$ is the negative-sequence component;
- $\vec{I}_{1(0)}$ is the zero-sequence component;

and by using the following operator

$$a = e^{j\frac{2\pi}{3}} = -\frac{1}{2} + j\frac{\sqrt{3}}{2} \text{ between } \vec{I}_1, \vec{I}_2, \text{ and } \vec{I}_3.$$

This principle, applied to a current system, is confirmed by a graphical representation (see fig. 23). For example, the graphical addition of the vectors produces, for, the following result:

$$\vec{I}_2 = a^2 \vec{I}_{1(1)} + a \vec{I}_{1(2)} + \vec{I}_{1(0)}$$

Currents \vec{I}_1 and \vec{I}_3 may be expressed in the same manner, hence the system:

$$\vec{I}_1 = \vec{I}_{1(1)} + \vec{I}_{1(2)} + \vec{I}_{1(0)}$$

$$\vec{I}_2 = a^2 \vec{I}_{1(1)} + a \vec{I}_{1(2)} + \vec{I}_{1(0)}$$

$$\vec{I}_3 = a \vec{I}_{1(1)} + a^2 \vec{I}_{1(2)} + \vec{I}_{1(0)}$$

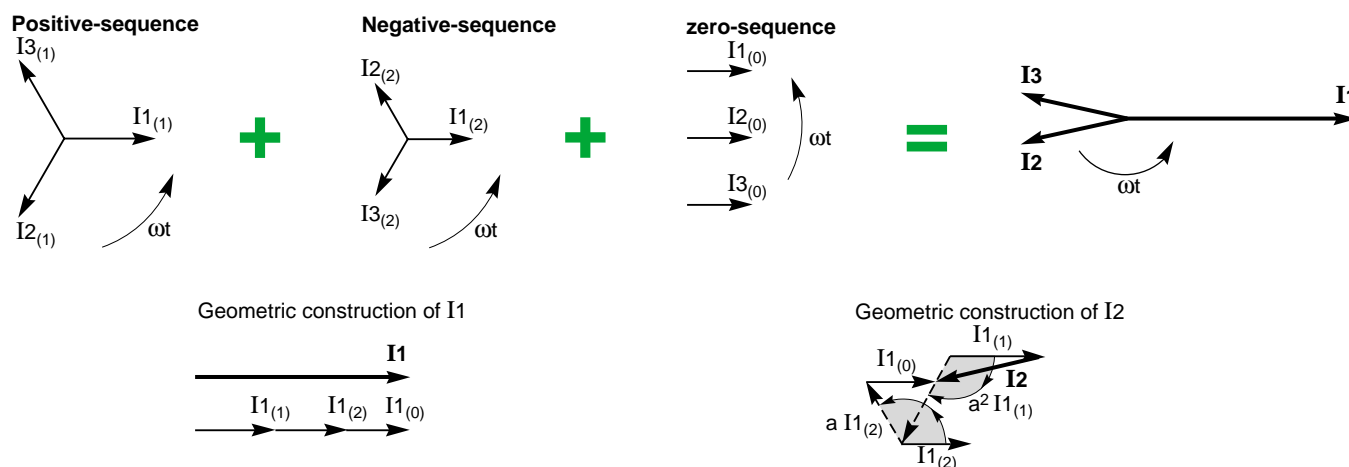


Fig. 23: graphical construction of the sum of three balanced three-phase systems (positive-sequence, negative-sequence and zero-sequence).

These symmetrical current components are related to the symmetrical voltage components by the corresponding impedances:

$$Z_{(1)} = \frac{V_{(1)}}{I_{(1)}}, Z_{(2)} = \frac{V_{(2)}}{I_{(2)}} \text{ and } Z_{(0)} = \frac{V_{(0)}}{I_{(0)}}$$

These impedances may be defined from the characteristics (supplied by the manufacturers) of the various elements in the given electrical network. Among these characteristics, we can note that $Z_{(2)} \approx Z_{(1)}$, except for rotating machines, whereas $Z_{(0)}$ varies depending on each element (see **fig. 24**).

For further information on this subject, a detailed presentation of this method for calculating solid and impedance fault currents is contained in the "Cahier Technique" n° 18 (see the appended bibliography).

Elements	$Z_{(0)}$	
Transformer (seen from secondary winding)		
No neutral	∞	
Yyn or Zyn	free flux	∞
	forced flux	10 to 15 $X_{(1)}$
Dyn or YNyn primary D or Y + zn	$X_{(1)}$	
		0.1 to 0.2 $X_{(1)}$
Machine		
Synchronous	$\approx 0.5 Z_{(1)}$	
Asynchronous	≈ 0	
Line	$\approx 3 Z_{(1)}$	

Fig. 24: zero-sequence characteristic of the various elements in an electrical network.

3.3 Calculation as defined by IEC 60909

Standard IEC 60909 defines and presents a method implementing symmetrical components, that may be used by engineers not specialised in the field.

The method is applicable to electrical networks with a rated voltage of less than 230 kV and the standard explains the calculation of minimum and maximum short-circuit currents. The former is required in view of calibrating overcurrent protection devices and the latter is used to determine the rated characteristics for the electrical equipment.

In view of its application to LV networks, the standard is accompanied by application guide IEC 60781.

Procedure

1- Calculate the equivalent voltage at the fault location, equal to $c U_n / \sqrt{3}$ where c is a voltage factor required in the calculation to account for:

- voltage variations in space and in time;
- possible changes in transformer tapplings;
- subtransient behaviour of generators and motors.

Rated voltage U_n	Voltage factor c for calculation of	
	$I_{sc} \text{ max.}$	$I_{sc} \text{ min.}$
LV		
230 - 400 V	1	0.95
Others	1.05	1
HV		
1 to 230 kV	1.1	1

Fig. 25: values for voltage factor c (see IEC 60909).

Depending on the required calculations and the given voltage levels, the standardised voltage levels are indicated in **figure 25**.

2- Determine and add up the equivalent positive-sequence, negative-sequence and zero-sequence impedances upstream of the fault location.

3- Calculate the initial short-circuit current using the symmetrical components. Practically speaking and depending on the type of fault, the equations required for the calculation of the I_{sc} are indicated in the table in **figure 26**.

4- Once the I_{sc} (I_k'') value is known, calculate the other values such as the peak I_{sc} value, the steady-state I_{sc} value and the maximum, steady-state I_{sc} value.

Effect of the distance separating the fault from the generator

When using this method, two different possibilities must always be considered:

■ the short-circuit is away from the generator, the situation in networks where the short-circuit currents do not have a damped, alternating component.

This is generally the case in LV networks, except when high-power loads are supplied by special HV substations;

■ the short-circuit is near the generator (see fig. 11), the situation in networks where the short-circuit currents do have a damped, alternating component. This generally occurs in HV systems, but may occur in LV systems when, for example, an emergency generator supplies priority outgoers.

The main differences between these two cases are:

- for short-circuits away from the generator:
 - the initial (I_k''), steady-state (I_k) and breaking (I_b) short-circuit currents are equal ($I_k'' = I_k = I_b$);

Type of short-circuit	I_k'' General situation	Fault occurring far from the generators
Three-phase (any Z_e)	$= \frac{c Un}{\sqrt{3} Z_{(1)} }$ <p>In both cases, the short-circuit current depends only on $Z_{(1)}$, which is generally replaced by Z_k, the short-circuit impedance at the fault location, defined by $Z_k = \sqrt{R_k^2 + X_k^2}$ where R_k is the sum of the resistances of one phase, connected in series; X_k is the sum of the reactances of one phase, connected in series.</p>	$= \frac{c Un}{\sqrt{3} Z_{(1)} }$
Phase-to-phase clear of earth ($Z_e = \infty$)	$= \frac{c Un}{ Z_{(1)} + Z_{(2)} }$	$= \frac{c Un}{2 Z_{(1)} }$
Phase-to-earth	$= \frac{c Un \sqrt{3}}{ Z_{(1)} + Z_{(2)} + Z_{(0)} }$	$= \frac{c Un \sqrt{3}}{ 2 Z_{(1)} + Z_{(0)} }$
Phase-to-phase-to-earth (Z_{sc} between phases = 0)	$= \frac{c Un \sqrt{3} Z_{(2)} }{ Z_{(1)} Z_{(2)} + Z_{(2)} Z_{(0)} + Z_{(1)} Z_{(0)} }$	$= \frac{c Un \sqrt{3}}{ Z_{(1)} + 2 Z_{(0)} }$

Symbols used in this table

- phase-to-phase rms voltage of the three-phase network = U
- modulus of the short-circuit current = I_k''
- symmetrical impedances = $Z_{(1)}$, $Z_{(2)}$, $Z_{(0)}$

- short-circuit impedance = Z_{sc}
- earth impedance = Z_e .

Fig. 26: Short-circuit values depending on the positive-sequence, negative-sequence & zero-sequence impedances of the given network (see IEC 60909).

- the positive-sequence ($Z_{(1)}$) and negative-sequence ($Z_{(2)}$) impedances are equal ($Z_{(1)} = Z_{(2)}$);
 - for short-circuits near the generator:
 - the short-circuit currents are not equal, in fact the relationship is $I_k < I_b < I_k''$;
 - the positive-sequence impedance ($Z_{(1)}$) is not necessarily equal to the negative-sequence impedance ($Z_{(2)}$).
- Note however that asynchronous motors may also add to a short-circuit, accounting for up to 30 % of the network I_{sc} for the first 30 milliseconds, in which case $I_k'' = I_k = I_b$ no longer holds true.

Conditions to consider when calculating the maximum and minimum short-circuit currents

- Calculation of the **maximum** short-circuit currents must take into account the following points:
 - application of the correct voltage factor c corresponding to calculation of the maximum short-circuit currents;
 - among the assumptions and approximations mentioned in this document, only those leading to a conservative error should be used;

- the resistances per unit length R_L of lines (overhead lines, cables, phase and neutral conductors) should be calculated for a temperature of 20 °C;
- Calculation of the minimum short-circuit currents requires:
 - applying the voltage factor c corresponding to the minimum permissible voltage on the network;
 - selecting the network configuration, and in some cases the minimum contribution from sources and network feeders, which result in the lowest short-circuit current at the fault location:
 - taking into account the impedance of the busbars, the current transformers, etc.;
 - neglecting the motors;
 - considering resistances R_L at the highest foreseeable temperature:

$$R_L = \left[1 + \frac{0.004}{^\circ\text{C}} (\theta_e - 20^\circ\text{C}) \right] R_{L20}$$

where R_{L20} is the resistance at 20 °C; θ_e is the permissible temperature (°C) for the conductor at the end of the short-circuit.

The factor 0.004 / °C is valid for copper, aluminium and aluminium alloys.

3.4 Equations for the various currents

Initial short-circuit current I_k''

The different initial short-circuit currents I_k'' are calculated using the equations in the table in figure 26.

Peak value i_p of the short-circuit current

In no meshed systems, the peak value i_p of the short-circuit current may be calculated for all types of faults using the equation:

$$i_p = K \sqrt{2} I_k''$$

I_k'' = is the initial short-circuit current;

K is a factor depending on the R / X ratio and defined in the graph in figure 9, or using the following approximate calculation:

$$K = 1.02 + 0.98 e^{-\frac{3R}{X}}$$

Short-circuit breaking current I_b

Calculation of the short-circuit breaking current I_b is required only when the fault is near the generator and protection is ensured by time-delayed circuit breakers. Note that this current is used to determine the breaking capacity of these circuit breakers.

This current may be calculated with a fair degree of accuracy using the following equation:

$I_b = \mu I_k''$ where μ is a factor defined by the minimum time delay t_{min} and the

I_k'' / I_r ratio (see [fig. 27](#)) which expresses the influence of the subtransient and transient reactances with I_r as the rated current of the generator.

Steady-state short-circuit current I_k

The amplitude of the steady-state short-circuit current I_k depends on generator saturation influences and calculation is therefore less accurate than for the initial symmetrical current I_k'' . The proposed calculation methods produce a sufficiently accurate estimate of the upper and lower limits, depending on whether the short-circuit is supplied by a generator or a synchronous machine.

■ The maximum steady-state short-circuit current, with the synchronous generator at its highest excitation, may be calculated by:

$$I_{k_{max}} = \lambda_{max} I_r$$

■ The minimum steady-state short-circuit current is calculated under no-load, constant (minimum) excitation conditions for the synchronous generator and using the equation:

$I_{k_{min}} = \lambda_{min} I_r$ where I_r is the rated current at the generator terminals;

λ is a factor defined by the saturation inductance $X_{d sat}$.

The λ_{max} and λ_{min} values are indicated in [figure 28](#) for turbo-generators and in [figure 29](#) for machines with salient poles.

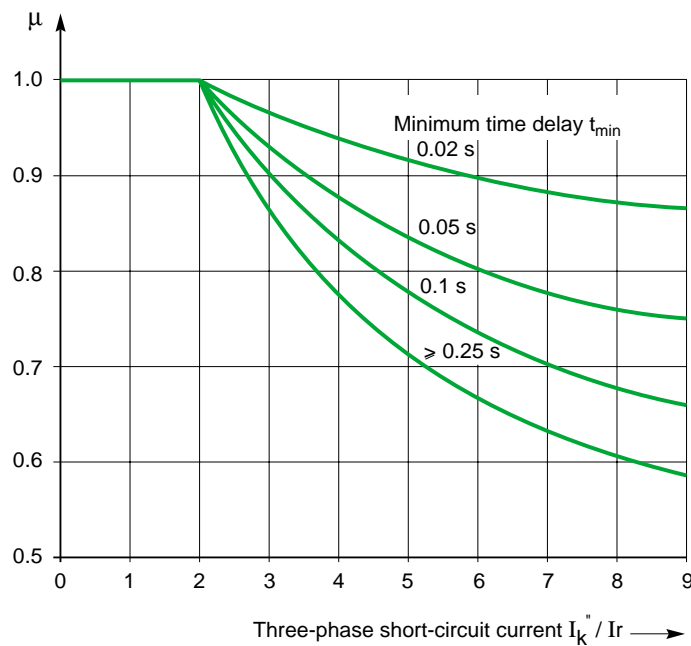


Fig. 27: factor μ used to calculate the short-circuit breaking current I_b (see IEC 60909).

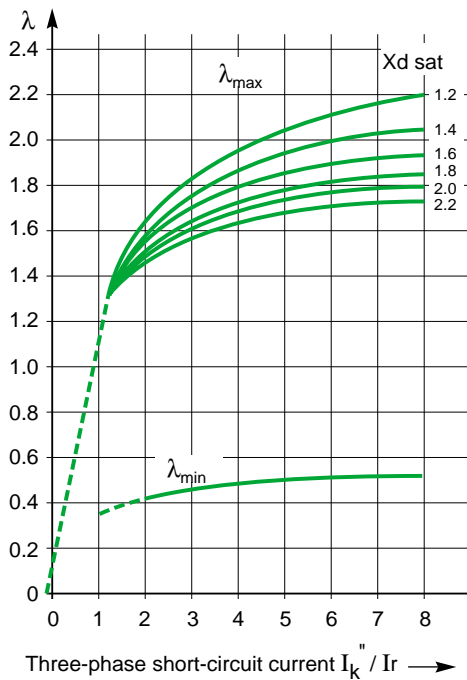


Fig. 28: factors λ_{max} and λ_{min} for turbo-generators (see IEC 60909).

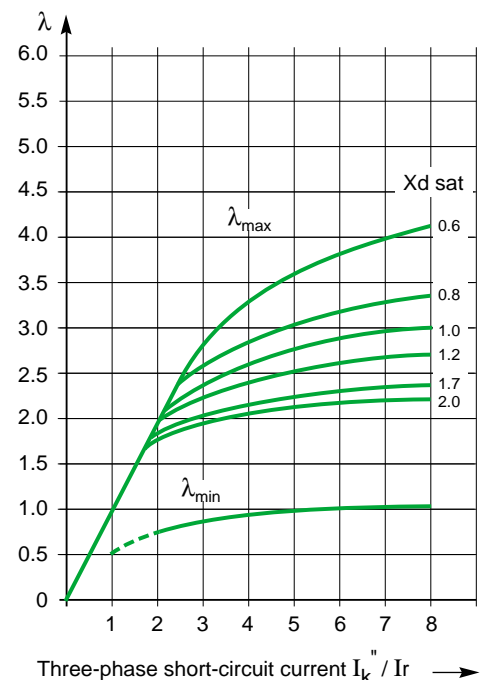


Fig. 29: factors λ_{max} and λ_{min} for generators with salient poles (see IEC 60909).

3.5 Calculation example

Problem

Consider four networks, three 5 kV networks and one 15 kV network, supplied via a 30 kV network by transformers in substation E (see fig. 30). During construction of line GH, calculation of the breaking capacity of circuit breaker M is requested.

The following information is available:

- only the secondary windings of the transformers in substation E are earthed;
- for a 30 kV line, the reactance value is $0.35 \Omega / \text{km}$ (positive-sequence and negative-sequence conditions) and $3 \cdot 0.35 \Omega / \text{km}$ (zero-sequence conditions);
- the short-circuit reactance is 6 % for the transformers in substation E and 8 % for the other transformers;
- the factor c for U is set to 1;
- all loads connected to points F and G are essentially passive;
- all resistances are negligible with respect to the reactances.

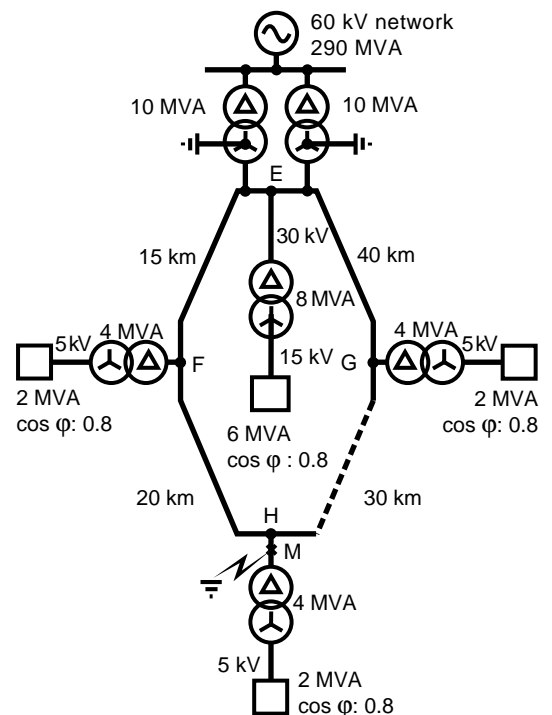


Fig. 30

Solution

■ On the basis of the positive-sequence and negative-sequence diagrams (see **fig. 31**), the following may be calculated:

$$a = \frac{U^2}{S_{sc}} = \frac{30^2}{290} \Rightarrow j 3.1 \Omega$$

$$b = u_{sc} \frac{U^2}{S_n} = \frac{6}{100} \times \frac{30^2}{10} \Rightarrow j 5.4 \Omega$$

$$c1 = 0.35 \times 40 \Rightarrow j 14 \Omega$$

$$c2 = 0.35 \times 30 \Rightarrow j 10.5 \Omega$$

$$c3 = 0.35 \times 20 \Rightarrow j 7 \Omega$$

$$c4 = 0.35 \times 15 \Rightarrow j 5.25 \Omega$$

$$d = u_{sc} \frac{U^2}{S_n} = \frac{8}{100} \times \frac{30^2}{8} \Rightarrow j 9 \Omega$$

$$e = \frac{U^2}{S} \times 0.6 = \frac{30^2}{6} \times 0.6 \Rightarrow j 90 \Omega$$

$$f = u_{sc} \frac{U^2}{S_n} = \frac{8}{100} \times \frac{30^2}{4} \Rightarrow j 18 \Omega$$

$$g = \frac{U^2}{S} \times 0.6 = \frac{30^2}{2} \times 0.6 \Rightarrow j 270 \Omega$$

■ Note on the zero-sequence diagram (see **fig. 32**):

□ the delta windings of the transformers in substation E block zero-sequence currents, i.e. the network is not affected by them;

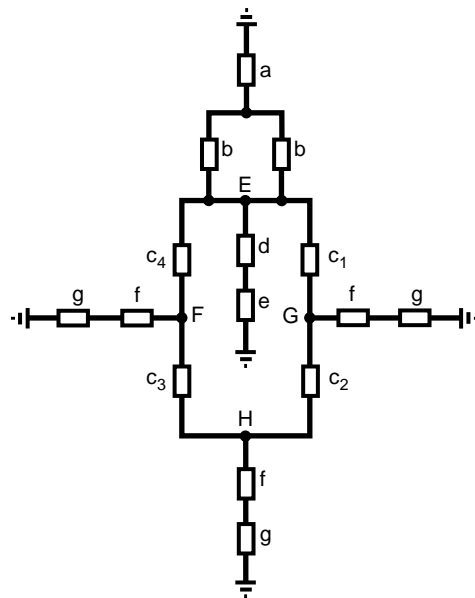


Fig. 31.

□ similarly, the transformers in the substations F, H and G, due to their delta windings, are not affected by the zero-sequence currents and, therefore, have an infinite impedance for the fault.

$$b' = b1 = j 5.4 \Omega$$

$$c'1 = 3 c1 = j 42 \Omega$$

$$c'2 = 3 c2 = j 31.5 \Omega$$

$$c'3 = 3 c3 = j 21 \Omega$$

$$c'4 = 3 c4 = j 15.75 \Omega$$

$$d' = \infty$$

$$f' = \infty$$

■ Calculations may therefore be made using two simplified diagrams:

□ with line GH open (see **fig. 33**):

$$Z_{(1)} = Z_{(2)} = j 17.25 \Omega$$

This result is obtained by successive calculations as shown in **figure 34**.

A similar calculation for the zero-sequence diagram gives the result:

$$Z_{(0)} = j 39.45 \Omega$$

$$I_{sc3} = \frac{c U_n}{|Z_{(1)}| \sqrt{3}} \approx 1.104 \text{ kA}$$

$$I_{sc1} = \frac{c U_n \sqrt{3}}{|Z_{(1)} + Z_{(2)} + Z_{(0)}|} \approx 0.773 \text{ kA}$$

Note the network is HV, hence coefficient $c = 1.1$.

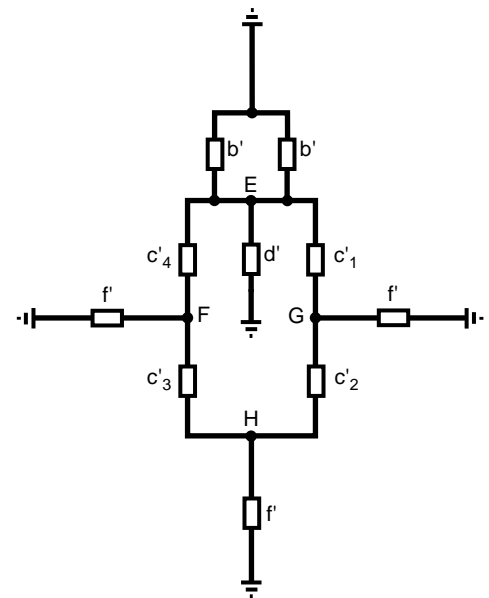


Fig. 32.

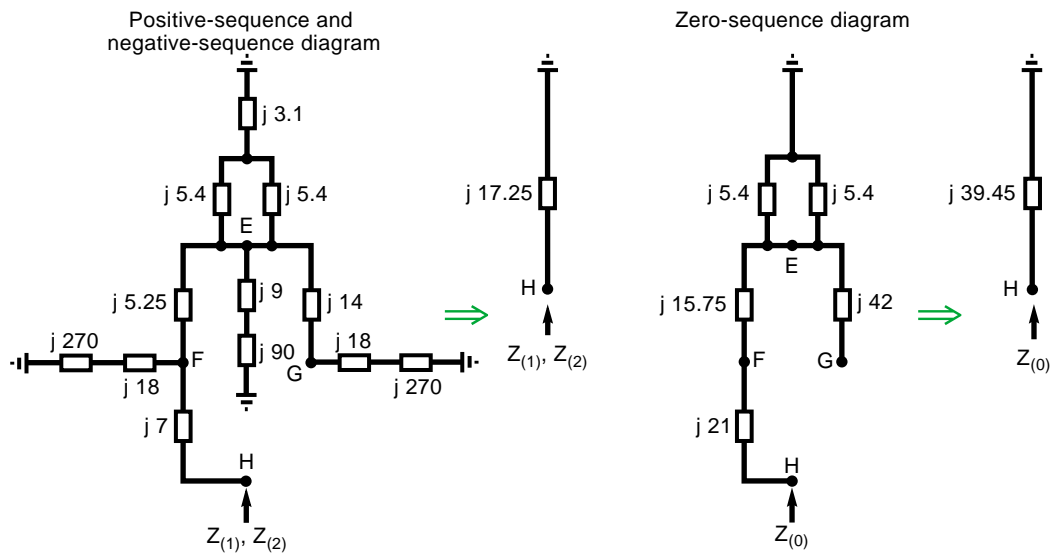


Fig. 33.

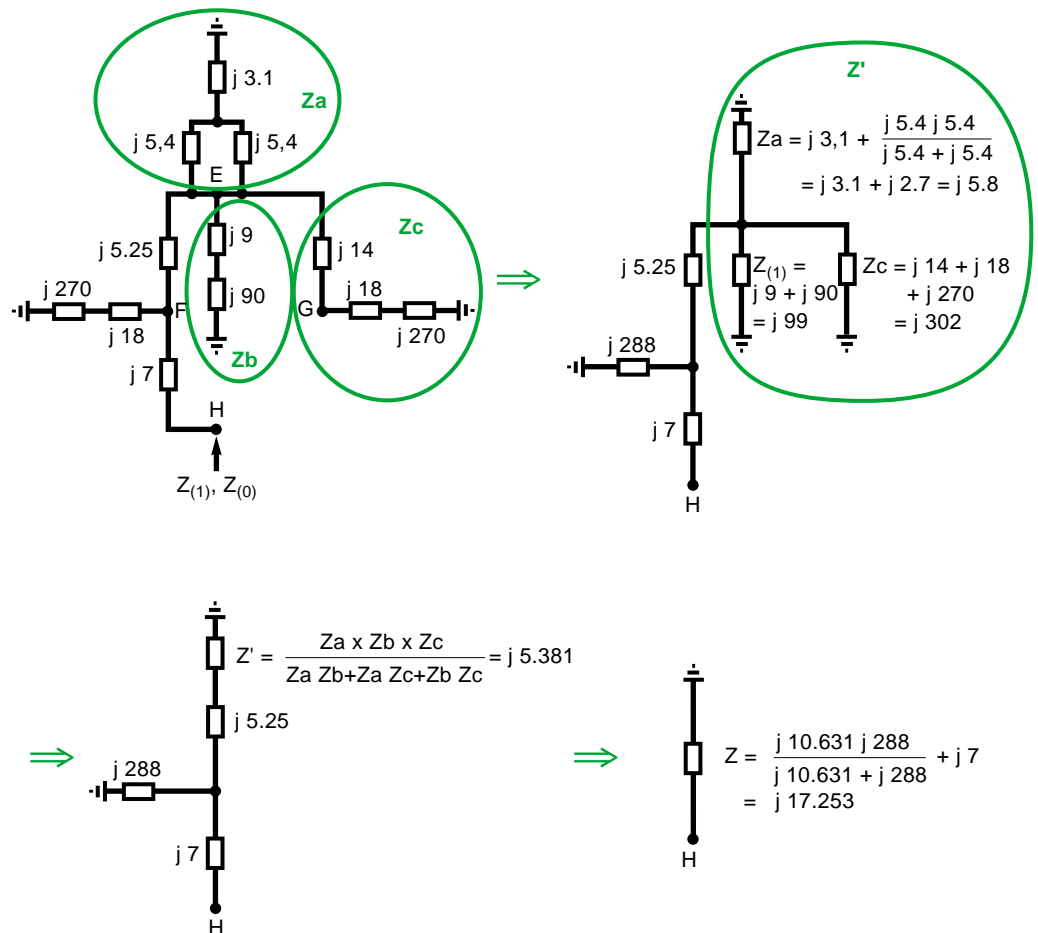


Fig. 34.

□ with line GH closed (see **fig. 35**):

$$Z_{(1)} = Z_{(2)} = j 13.05 \Omega$$

$$Z_{(0)} = j 27.2 \Omega$$

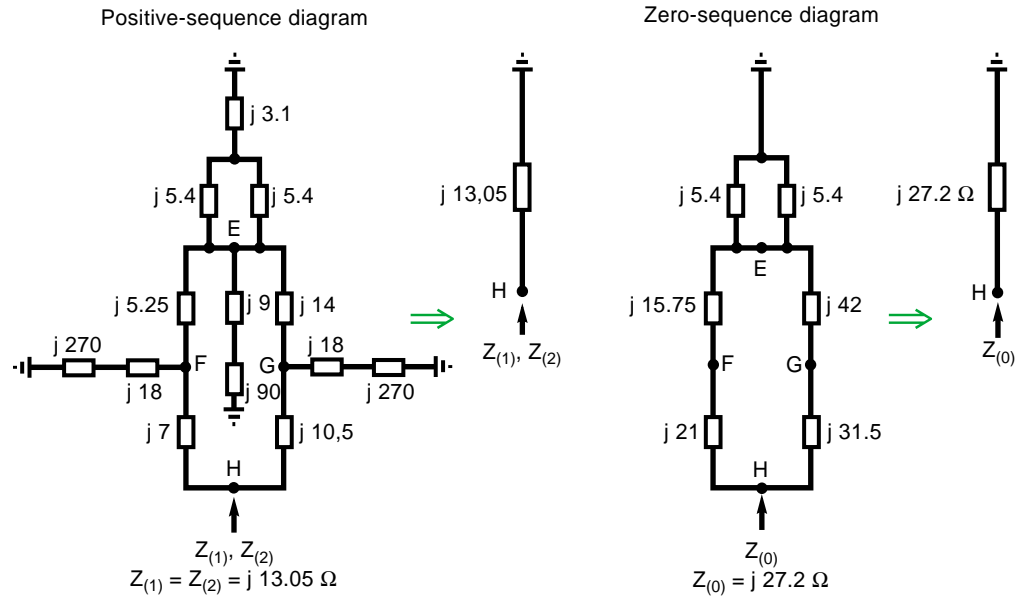
$$I_{sc3} = 1.460 \text{ kA}$$

$$I_{sc1} = 1.072 \text{ kA}$$

Given the highest short-circuit current (**$I_{sc3} = 1.460 \text{ kA}$**), the line circuit breaker at point M must be sized for:

$$P = U I \sqrt{3} = 30 \times 1.460 \times \sqrt{3}$$

$$P \approx \mathbf{76 \text{ MVA.}}$$



4 Computerised calculations and conclusion

Various methods for the calculation of short-circuit currents have been developed. Some have been included in a number of standards and are consequently included in this "Cahier Technique" publication as well.

Several standardised methods were designed in such a way that short-circuit currents could be calculated by hand or using a small calculator. When computerised scientific calculations became a possibility in the 1970's, electrical-installation designers devised software for their particular needs. This software was initially run on mainframe computer systems, then on minicomputers, but was difficult to use, and therefore limited to a small number of experts.

This software was finally transferred to the PC microcomputing environment, proving much easier to use. Today, a wide range of software packages are available which comply with the applicable standards defining the calculation of Isc currents in LV applications, for example

Ecodial, a program designed and marketed by Schneider Electric.

All computer programs designed to calculate short-circuit currents are predominantly concerned with determining the required breaking and making capacities of switchgear and the electro-mechanical withstand capabilities of equipment.

Other software is used by experts specialising in network design, for example, research on the dynamic behaviour of electrical networks. Such computer programs can be used for precise simulations of electrical phenomena over time and their use is now spreading to include the entire electro-mechanical behaviour of networks and installations.

Remember, however, that all software, whatever its degree of sophistication, is only a tool. To ensure correct results, it should be used by qualified professionals who have acquired the relevant knowledge and expertise.

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- Electrical Installation Guide, Ref.: MD1ELG2E (information on this 400 page publication is obtainable on www.schneiderformation.com)

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